UNIT 6 - MENSURATION

20

Perimeter and Area of Plane figures

POINTS TO REMEMBER

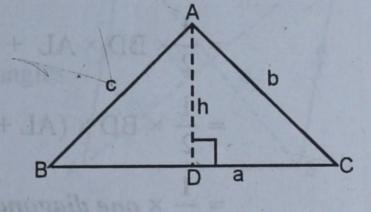
- 1. Perimeter: The perimeter of a plane figure is the length of its boundary, i.e., the sum of its sides. The unit of perimeter is the same as the unit of length.
- 2. Area: The area of a plane figure is the measure of the surface enclosed by its boundary, i.e., the surface enclosed by its sides.

It is measured in square units such as square centimetres or square metres, written as cm² or m² respectively.

- 3. PERIMETER AND AREA OF TRIANGLES
- A. Area of a Triangle = $\frac{1}{2}$ × Base × Corresponding Height.

Any side of the trainingel may be taken as base and the length of perpendicular from the opposite vertex to the base is the corresponding height.

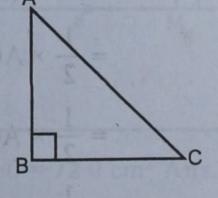
In given figure, Area of \triangle ABC = $(\frac{1}{2} \times BC \times AD)$ sq. units Perimeter = (a + b + c) units



B Hero's Formula: Let a, b, c, be the lengths of the sides of a triangle and let $s = \frac{1}{2}(a+b+c)$, called semi-perimeter of the triangle. Then.

Area of the Triangle = $\sqrt{s(s-a)(s-b)(s-c)}$ sq. units.

- C. For a Right-Angled \triangle ABC in which \angle B = 90°, we have :
 - (i) $AC^2 = AB^2 + BC^2$ (Pythagoras Theorem)
 - (ii) Area of \triangle ABC = $\frac{1}{2}$ × (Product of sides containing the right angle) = $\left(\frac{1}{2} \times BC \times AB\right)$ sq. units



- (iii) Perimeter = (Sum of three sides) units
- D. For An Equilateral Triangles of Side a, we have :

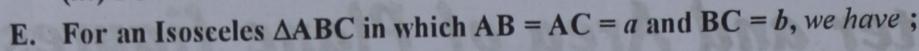
(i) Height =
$$\left(\frac{\sqrt{3}}{2}a\right)$$
 units.

$$h = \sqrt{a^2 - \left(\frac{a}{2}\right)^2}$$

(ii) Area =
$$\left(\frac{\sqrt{3}}{4}a^2\right)$$
 sq. units

$$\left[:: A = \frac{1}{2} \times a \times h \right]$$

(iii) Perimeter = 3a units.



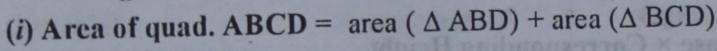
(i) Height =
$$\frac{\sqrt{4a^2 - b^2}}{2}$$
 units.
$$\left[\because h = \sqrt{a^2 - \left(\frac{b}{2}\right)^2} \right]$$

(ii) Area =
$$\left(\frac{1}{4}b\sqrt{4a^2-b^2}\right)$$
 sq. units $\left[\because A = \frac{1}{2} \times b \times h\right]$

(iii) Perimeter = (2a + b) units.

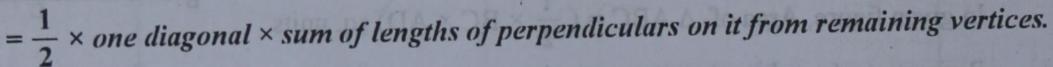
4. PERIMETER AND AREA OF QUADRILATERALS

A. Area of Quadrilateral when one diagonal and perpendiculars from remaining vertices to the diagonal are given



$$= \frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$$

$$= \frac{1}{2} \times BD \times (AL + CM)$$



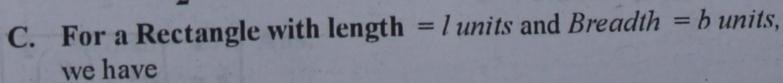
(ii) Perimeter = sum of four sides units

B. Area of a Quadrilateral whose Diagonals Intersect At Right Angles

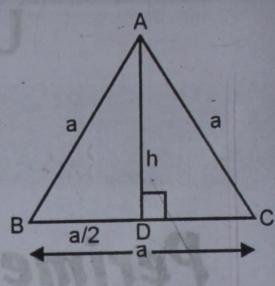
Let the diagonals AC and BD of quad. ABCD intersect at O at right angles. Then,

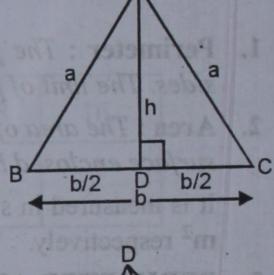
Area of quad. ABCD.

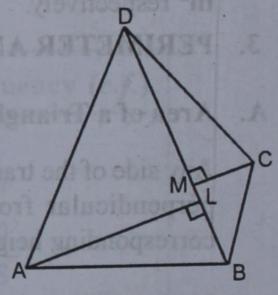
= Area (
$$\triangle$$
 ABC) + Area (\triangle ACD)
= $\frac{1}{2} \times AC \times BO + \frac{1}{2} \times AC \times OD$
= $\frac{1}{2} \times AC \times (BO + OD)$
= $\frac{1}{2} \times AC \times BD$
= $\frac{1}{2} \times (Product of its diagonals)$ square units.

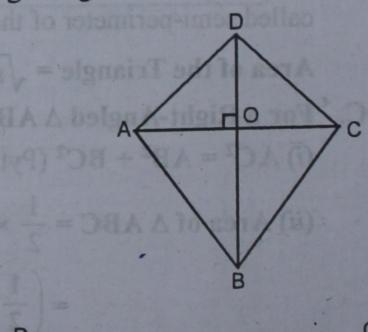


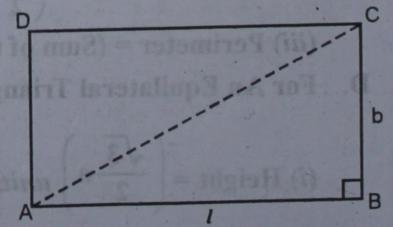
(i) Perimeter = 2 (Length + Breadth) =
$$2(l+b)$$
 units.







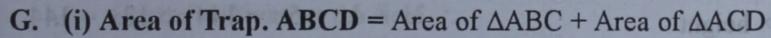




- (ii) Area = (Length \times Breadth) = $(l \times b)$ sq. units.
- (iii) Diagonal = $\sqrt{1^2 + b^2}$ units.
- D. For a square with side a units, we have:
 - (i) Perimeter = $(4 \times \text{side}) = 4 a \text{ units.}$
 - (ii) Area = $(side)^2 = a^2 sq.$ units.
 - (iii) Area = $\frac{1}{2}$ × (Diagonal)² sq. units.
 - (iv) Diagonal = $\sqrt{2}$ a units = $\sqrt{2 \times \text{Area units.}}$.
- E. Area of a Parallelogram = Base × Height.
 - (i) Area of $\|gm ABCD = AB \times DL$ = $AD \times BM$.
 - (ii) Perimeter = 2 (AB + BC) units
- F. Area of Rhombus = $\frac{1}{2}$ × Product of its diagonals.

$$= \left(\frac{1}{2} \times d_1 \times d_2\right) sq. \ units.$$

Remark. The diagonals of a rhombus bisect each other at right angles.



$$= \frac{1}{2} \times AB \times h + \frac{1}{2} \times CD \times h$$

$$= \frac{1}{2} \times (AB + CD) \times h$$

$$= \frac{1}{2} \times (Sum \ of \ parallel \ sides)$$

× (Distance between them) sq. units

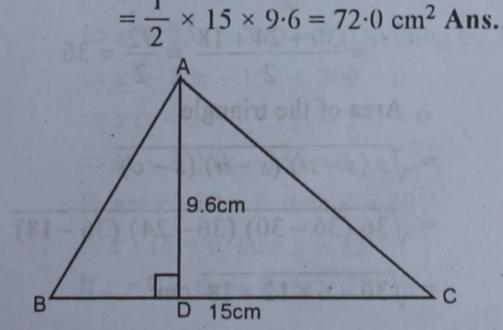
(ii) Perimeter = sum of four sides units

Note:
$$\sqrt{2} = 1.414$$
 or 1.41
 $\sqrt{3} = 1.732$ or 1.73

a

EXERCISE 20 (A)

- Q. 1. Find the area of a triangle whose base is 15 cm and the corresponding height is 9.6 cm.
- Sol. Base BC of triangle ABC = 15 cm and its altitude AD = 9.6 cm
 - $\therefore \text{ Area of } \triangle \text{ ABC} = \frac{1}{2} \text{ base} \times \text{ altitude}$



- Q. 2. Find the area of the triangle whose sides are 13 cm, 14 cm and 15 cm. Also find the height of the triangle corresponding to the longest side.
- Sol. Let a = 13 cm, b = 14 cm and c = 15 cm $\therefore s = \frac{a+b+c}{2} = \frac{13+14+15}{2}$ $= \frac{42}{2} = 21$ cm.

:. Area of triangle

$$= \sqrt{s (s-a) (s-b) (s-c)}$$

$$= \sqrt{21 (21-13) (21-14) (21-15)}$$

$$= \sqrt{21 \times 8 \times 7 \times 6} \text{ cm}^2$$

$$= \sqrt{3 \times 7 \times 2 \times 2 \times 2 \times 7 \times 2 \times 3}$$

$$= 2 \times 2 \times 3 \times 7 = 84 \text{ cm}^2$$
Let the height on the longest side

h = 15 cm then,

area of
$$\Delta = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow 84 = \frac{1}{2} \times 15 \times h$$

$$\Rightarrow h = \frac{84 \times 2}{15} = \frac{56}{5} = 11.2 \text{ cm. Ans.}$$

- Q. 3. Find the area of the triangle whose sides are 30 cm, 24 cm and 18 cm. Also find the length of the altitude corresponding to the smallest side of the triangle.
 - Sol. Let sides of triangle are a = 30 cm, b = 24 cm and c = 18 cm $and s = \frac{a+b+c}{2}$ $= \frac{30+24+18}{2} = \frac{72}{2} = 36$ $\therefore \text{ Area of the triangle}$

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{36(36-30)(36-24)(36-18)}$$

$$= \sqrt{36 \times 6 \times 12 \times 18} \text{ cm}^2$$

$$= 2 \times 3 \times 2 \times 3 \times 2 \times 3 = 216 \text{ cm}^2$$

Let the length of altitude on the smallest side of 18 cm = h.

Then area of triangle

$$=\frac{1}{2} \times \text{base} \times \text{altitude}$$

$$\Rightarrow 216 = \frac{1}{2} \times 18 \times h$$

$$\Rightarrow 9h = 216 \Rightarrow h = \frac{216}{9} = 24$$

:. Altitude = 24 cm. Ans.

- Q. 4. The lengths of the sides of a triangle are in the ratio 3: 4: 5 and its perimeter is 144 cm. Find the area of the triangle.
- Sol. Ratio in sides = 3:4:5 and Perimeter = 144 cm

Let the sides are 3x, 4x and 5x

$$3x + 4x + 5x = 144 \Rightarrow 12x = 144$$

$$\Rightarrow x = \frac{144}{12} = 12$$

:. Sides are 3×12 , 4×12 , 5×12 *i.e.* 36 cm, 48 cm and 60 cm.

$$\therefore s = \frac{\text{sum of sides}}{2} = \frac{144}{2} = 72$$

:. Area of the triangle

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{72 (72 - 36) (72 - 48) (72 - 60)}$$

$$= \sqrt{72 \times 36 \times 24 \times 12} \text{ cm}^2$$

$$= \sqrt{36 \times 2 \times 36 \times 2 \times 12 \times 12} \text{ cm}^2$$

$$= 2 \times 36 \times 12 \text{ cm}^2 = 864 \text{ cm}^2 \text{ Ans.}$$

Q.5. The perimeter of triangular field is 540 m and its sides are in the ratio 25: 17: 12. Find the area of the triangle. Also, find the cost of cultivating the field at Rs. 24.60 per 100 m².

Ratio of sides = 25 : 17 : 12

Let sides be 25x, 17x, 12x

Then 25x + 17x + 12x = 540

$$\Rightarrow$$
 54x = 540 \Rightarrow x = 10

:. Sides are 25×10 , 17×10 , 12×10 = 250 m, 170 m, 120 m.

$$\therefore s = \frac{\text{sum of sides}}{2} = \frac{540}{2} = 270$$

:. Area of the triangular field

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{270 (270 - 250) (270 - 170) (270 - 120)}$$

$$= \sqrt{270 \times 20 \times 100 \times 150}$$

$$= \sqrt{3 \times 3 \times 3 \times 10 \times 2 \times 10 \times 2 \times 5 \times 10 \times 3 \times 5 \times 10}$$

$$= \sqrt{2 \times 3 \times 3 \times 5 \times 10 \times 10} \text{ m}^2$$

 $= 9000 \text{ m}^2$

Cost of cultivating the field

 $= Rs.24.60 per 100m^2$

$$\therefore \text{ Total cost} = \text{Rs.} \frac{9000 \times 24 \cdot 60}{100}$$

= Rs.
$$\frac{9000 \times 2460}{100 \times 100}$$
 = Rs. 2214 Ans.

- Q. 6. The base of a triangular field is twice its altitude. If the cost of cultivating the field at Rs. 14.50 per 100 m² is Rs. 52,200, find its base and altitude.
- Sol. Let altitude of the triangle = x

Then base = 2x

$$\therefore \text{ Area} = \frac{1}{2} \text{ base} \times \text{altitude}$$

$$\Rightarrow \frac{1}{2} \times 2x \times x = x^2 \tag{i}$$

Total cost of cultivative of the field

$$= Rs. 52,200$$

Rate of cultivating

$$= Rs. 14.50 per 100 m2$$

$$\therefore \text{ Area of the field} = \frac{52200 \times 100}{14 \cdot 50}$$

$$= \frac{52200 \times 100 \times 100}{1450} m^2$$

$$= 360000 \text{ m}^2 \qquad ...(ii)$$

From (i) and (ii)

$$\therefore x^2 = 360000 \implies x^2 = (600)^2$$

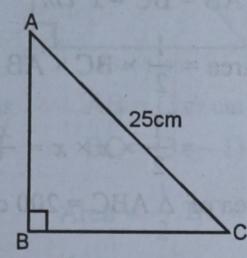
$$\Rightarrow x = 600$$

Hence Base = $2 \times 600 = 1200 \text{ m}$

and altitude = $600 \times 1 = 600 \text{ m Ans.}$

- Q. 7. The perimeter of a right triangle is 60 cm and its hypotenuse is 25 cm. Find the area of the triangle.
 - Sol. In right angled \triangle ABC,

 $\angle B = 90^{\circ}$, hypotenuse AC = 25cm and perimeter = 60 cm.



:.
$$AB + BC = 60 - 25 = 35 \text{ cm}$$

Let base
$$BC = x$$
 cm

Then altitude
$$AB = 35 - x$$

But
$$AC^2 = AB^2 + BC^2$$

(Pythagoras theorem)

$$\Rightarrow$$
 $(25)^2 = (35 - x)^2 + x^2$

$$\Rightarrow 625 = 1225 - 70x + x^2 + x^2$$

$$\Rightarrow 2x^2 - 70x + 1225 - 625 = 0$$

$$\Rightarrow 2x^2 - 70x + 600 = 0$$

$$\Rightarrow x^2 - 35x + 300 = 0$$
 (Dividing by 2)

$$\Rightarrow x^2 - 20x - 15x + 300 = 0$$

$$\Rightarrow x(x-20)-15(x-20)=0$$

$$\Rightarrow (x-20)(x-15)=0$$

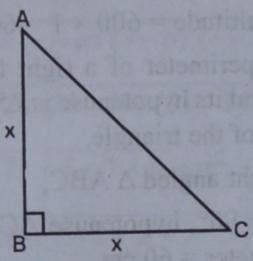
Either
$$x - 20 = 0$$
, then $x = 20$

or
$$x - 15 = 0$$
, then $x = 15$

If
$$x = 20$$
, then, Base = 20 cm

and altitude = 35 - 20 = 15 cm If x = 15, then, Base = 15 cm and altitude = 35 - 15 = 20 cm Hence sides are 15cm, 20 cm. **Ans.**

- Q. 8. Find the length of hypotenuse of an isosceles right angled triangle having an area of 200 cm² (Take $\sqrt{2} = 1.414$).
 - Sol. In right angled isosceles triangle ABC, $\angle B = 90^{\circ}$ and AB = BC



Let $AB = BC = x \ cm$

$$\therefore \text{ Area} = \frac{1}{2} \times \text{BC} \times \text{AB}$$
$$= \frac{1}{2} \times x \times x = \frac{x^2}{2}$$

But area of \triangle ABC = 200 cm²

$$\therefore \frac{x^2}{2} = 200 \implies x^2 = 400 = (20)^2$$

$$\therefore x = 20$$

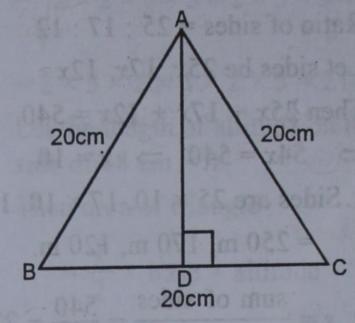
Now hypotenuse $AC = \sqrt{AB^2 + BC^2}$ $= \sqrt{(20)^2 + (20)^2}$ $= \sqrt{400 + 400} = \sqrt{800}$ $= \sqrt{2 \times 400}$ $= 20 \times \sqrt{2}$ cm $= 20 \times 1.414$ cm

= 28.280 cm

=28.28 cm Ans.

Q. 9. Calculate the area and the height of an equilateral triangle whose perimeter is 60 cm.

Sol. Perimeter of \triangle ABC = 60 cm



 $\therefore \text{ Each side} = \frac{60}{3} = 20 \text{cm}.$

Now altitude AD =
$$\frac{\sqrt{3}}{2}a$$

= $\frac{1.732}{2} \times 20 = 17.32$ cm.

and area of AABC

$$= \frac{\sqrt{3}}{4}a^2 = \frac{1.732}{4}(20^2) \text{ cm}^2$$
$$= \frac{1.732}{4} \times 400 = 173.2 \text{ cm}^2 \text{ Ans.}$$

- Q. 10. Find the perimeter and area of an equilateral triangle whose height is 12 cm Write your answers, correct to two decimal places.
 - Sol. Height of an equilateral triangle = 12 cmLet side of equilateral triangle = a

then height
$$(h) = \frac{\sqrt{3}}{2}a$$

$$\therefore \frac{\sqrt{3}}{2} a = 12 \implies a = \frac{12 \times 2}{\sqrt{3}} \text{ cm}$$

$$\Rightarrow a = \frac{24 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}}$$
$$= \frac{24 \times \sqrt{3}}{3} = 8\sqrt{3} \text{ cm}$$

Now perimeter of the triangle = 3a

=
$$3 \times 8\sqrt{3}$$
 cm
= 24 (1.732) cm

=41.568 cm

$$= 41.57 \text{ cm}$$

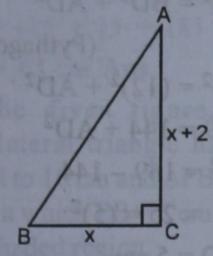
and area of the triangle =
$$\frac{\sqrt{3}}{4}a^2$$

= $\frac{1.732}{4} \times (8\sqrt{3})^2 \text{ cm}^2$
= $\frac{1.732}{4} \times 64 \times 3 \text{ cm}^2$
= $0.433 \times 192 \text{ cm}^2$
= 83.136 cm^2
= $83.14 \text{ cm}^2 \text{ Ans.}$

- Q. 11. The lengths of two sides of a right triangle containing the right angle differ by 2cm. If the area of the triangle is 24cm², find the perimeter of the triangle.
 - Sol. In right \triangle ABC, \angle C= 90°

Let
$$BC = x cm$$

Then
$$AC = x + 2 \text{ cm}$$
.



$$\therefore \text{ Area} = \frac{1}{2} \times \text{BC} \times \text{AC}$$

$$\Rightarrow 24 = \frac{1}{2}x(x+2)$$

$$\Rightarrow$$
 48 = $x^2 + 2x$

$$\Rightarrow x^2 + 2x - 48 = 0$$

$$\Rightarrow x^2 + 8x - 6x - 48 = 0$$

$$\Rightarrow x(x+8) - 6(x+8) = 0$$

$$\Rightarrow (x+8)(x-6)=0$$

Either x + 8 = 0, then x = -8 which is not possible

or
$$x - 6 = 0$$
, then $x = 6$

:. BC = 6 cm and AC =
$$6 + 2 = 8$$
 cm.

But
$$AB^2 = BC^2 + AC^2$$

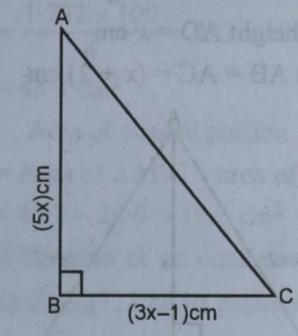
= $(6)^2 + (8)^2 = 36 + 64$
= $100 = (10)^2$

$$AB = 10 \text{ cm}$$

Now perimeter of the triangle
=
$$AB + BC + CA$$

= $10 + 6 + 8 \text{ cm} = 24 \text{ cm Ans.}$

- Q. 12. The sides of a right-angled triangle containing the right angle are (5x) cm and (3x 1) cm. If its area is 60 cm^2 , find its perimeter.
 - Sol. In right \triangle ABC, \angle B = 90° Area of triangle = 60 cm²



This
$$AB = (5x) \text{ cm}$$

and $BC = (3x - 1) \text{ cm}$

$$\therefore Area = \frac{1}{2} BC \times AB$$

$$\Rightarrow \qquad 60 = \frac{1}{2} \times (3x - 1) \times 5x$$

$$120 = 15x^2 - 5x$$

$$\Rightarrow 15x^2 - 5x - 120 = 0$$

$$\Rightarrow 3x^2 - x - 24 = 0$$

$$\Rightarrow$$
 $3x^2 - 9x + 8x - 24 = 0$

$$\Rightarrow 3x(x-3) + 8(x-3) = 0$$

$$\Rightarrow (x-3)(3x+8)=0$$

Either
$$x - 3 = 0$$
, then $x = 3$

or
$$3x + 8 = 0$$
,

then $x = -\frac{8}{3}$ which is not possible

:. AB =
$$5x = 5 \times 3 = 15$$
 cm and

$$BC = 3x - 1 = 3 \times 3 - 1 = 9 - 1 = 8 \text{ cm}$$

But
$$AC^2 = AB^2 + BC^2$$

(Pythagoras theorem)

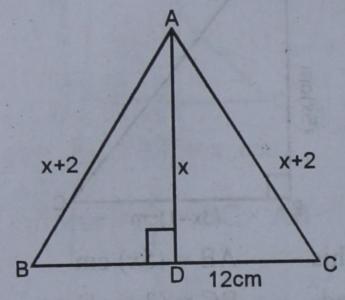
$$= (15)^2 + (8)^2 = 225 + 64$$
$$= 289 = (17)^2$$

$$\therefore$$
 AC = 17 cm.

Now perimeter of the triangle

$$= 15 + 8 + 17 = 40$$
 cm Ans.

- Q. 13. Each of the equal sides of an isosceles triangle is 2 cm more than its height and the base of the triangle is 12 cm. Find the area of the triangle.
 - Sol. Let height AD = x cm then AB = AC = (x + 2) cm



Base BC = 12 cm

:. BD = DC =
$$\frac{12}{2}$$
 = 6 cm

.: In right ΔABD,

$$AB^2 = BD^2 + AD^2$$

$$\Rightarrow$$
 $(x+2)^2 = (6)^2 + x^2$

$$\Rightarrow x^2 + 4x + 4 = 36 + x^2$$

$$\Rightarrow x^2 + 4x - x^2 = 36 - 4$$

$$\Rightarrow 4x = 32 \Rightarrow x = \frac{32}{4} = 8$$

$$\therefore$$
 AD = 8 cm

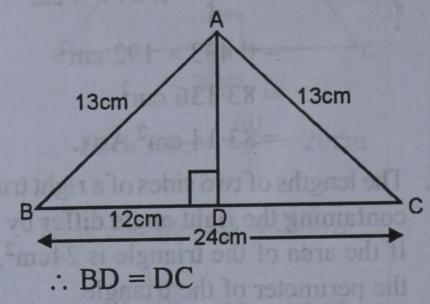
Now Area of AABC

$$= \frac{1}{2} \times \text{Base} \times \text{Altitude}$$

$$= \frac{1}{2} \times \text{BC} \times \text{AD}$$

$$= \frac{1}{2} \times 12 \times 8 \text{ cm}^2 = 48 \text{ cm}^2 \text{ Ans.}$$

- Q. 14. Find the area of an isosceles triangle, each of whose equal sides is 13 cm and base 24 cm.
 - Sol. $\triangle ABC$ is an isosceles triangle in which AB = AC = 13 cm and BC = 24 cm. $AD \perp BC$ which bisects BC in D.



$$=\frac{1}{2}BC = \frac{1}{2} \times 24 = 12 \text{ cm}$$

Now in right ΔABD,

$$AB^2 = BD^2 + AD^2$$

(Pythagoras Theorem)

$$\Rightarrow (13)^2 = (12)^2 + AD^2$$

$$\Rightarrow 169 = 144 + AD^2$$

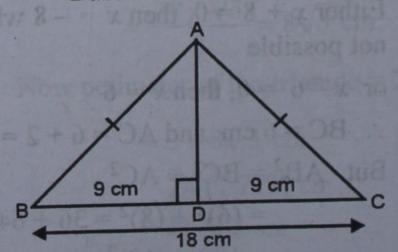
$$\Rightarrow AD^2 = 169 - 144$$
$$= 25 = (5)^2$$

$$\therefore$$
 AD = 5 cm

Now area of $\triangle ABC = \frac{1}{2}BC \times AD$

$$=\frac{1}{2} \times 24 \times 5 = 60 \text{ cm}^2$$
 Ans.

- Q. 15. The base of an isosceles triangle is 18 cm and its area is 108 cm². Find its perimeter.
 - Sol. Area of isosceles $\triangle ABC = 108 \text{ cm}^2$ Base BC = 18 cm



Let AD be its height,

Then, AD =
$$\frac{\text{Area} \times 2}{\text{Base}}$$

= $\frac{108 \times 2}{18}$ = 12 cm

In $\triangle ABC$, $AD \perp BC$

.. D is mid-point of BC

:. BD = DC =
$$\frac{18}{2}$$
 = 9 cm

$$\therefore AB^2 = BD^2 + AD^2$$

(Pythagoras Theorem)

$$= (9)^{2} + (12)^{2} = 81 + 144$$

= $225 = (15)^{2}$

$$\therefore$$
 AB = 15 cm.

But,
$$AC = AB = 15$$
 cm.

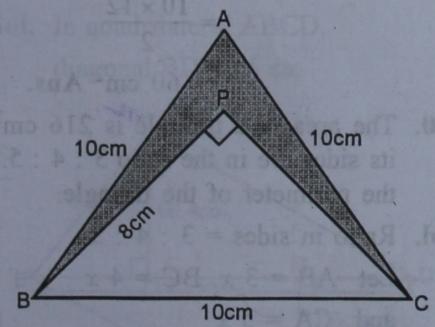
Now, perimeter of ΔABC

$$= AB + AC + BC$$

$$= (15 + 15 + 18)$$
 cm

= 48 cm Ans.

Q. 16. In the given figure, $\triangle ABC$ is an equilateral triangle having each side equal to 10 cm and $\triangle PBC$ is right angled at P in which PB = 8 cm. Find the area of the shaded region.



Sol. \triangle ABC is an equilateral triangle whose each side = 10 cm

 \triangle BPC is right angled triangle in which \angle P = 90° and PB = 8 cm

In right $\triangle PBC$, $BC^2 = PB^2 + PC^2$

(Pythagoras Theorem)

$$\Rightarrow (10)^2 = (8)^2 + PC^2$$

$$\Rightarrow$$
 100 = 64 + PC²

$$\Rightarrow$$
 PC² = 100 - 64 = 36 = (6)²

$$\therefore$$
 PC = 6 cm

Now area of $\triangle PBC = \frac{1}{2} \times PB \times PC$

$$= \frac{1}{2} \times 8 \times 6 = 24 \,\mathrm{cm}^2$$

and area of AABC

$$=\frac{\sqrt{3}}{4}a^2=\frac{1.732}{4}\times(10)^2\text{ cm}^2$$

$$= \frac{1.732 \times 100}{4} = 433 \times 100 \text{ cm}^2$$

 $= 43.3 \text{ cm}^2$

: Area of shaded portion

= Area of $\triangle ABC$ – area of $\triangle PBC$

$$= 43.3 - 24.0 = 19.3 \text{ cm}^2 \text{ Ans.}$$

- Q. 17. If the area of an equilateral triangle is $81\sqrt{3}$ cm², find its perimeter.
 - Sol. Let each side of equilateral triangle = a

$$\therefore \quad \text{Area} = \frac{\sqrt{3}}{4} a^2$$

$$\Rightarrow \frac{\sqrt{3}}{4}a^2 = 8\sqrt{3}$$

$$\Rightarrow a^2 = \frac{81 \times 4\sqrt{3}}{\sqrt{3}}$$

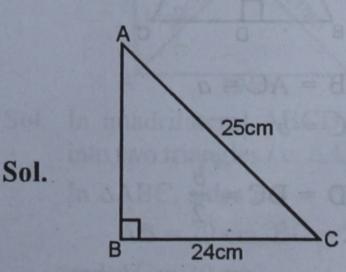
$$\Rightarrow a^2 = 324 = (18)^2$$

$$\therefore$$
 $a = 18 \text{ cm}$

Now perimeter = $3 a = 3 \times 18$

= 54 cm Ans.

Q. 18. The base of right – angled triangle is 24 cm and its hypotenuse is 25 cm. Find the area of the triangle.



In
$$\triangle ABC$$
, $\angle B = 90^{\circ}$

$$BC = 24 \text{ cm}$$

and
$$AC = 25$$
 cm

But
$$AC^2 = AB^2 + BC^2$$

(Pythagoras Theorem)

$$\Rightarrow$$
 (25)² = AB² + (24)²

$$\Rightarrow 625 = AB^2 + 576$$

$$\Rightarrow AB^2 = 625 - 576$$
$$= 49 = (7)^2$$

$$\therefore$$
 AB = 7 cm

Now area of AABC

$$=\frac{1}{2}$$
 Base × Altitude

$$= \frac{1}{2} \times BC \times AB$$

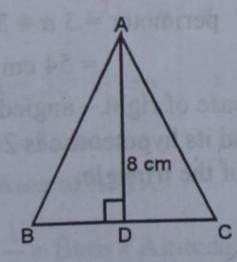
$$=\frac{1}{2}\times24\times7\,\mathrm{cm}^2$$

$$= 84 \text{ cm}^2 \text{ Ans.}$$

- Q. 19. The altitude drawn to the base of an isosceles triangle is 8 cm and the perimeter is 32 cm. Find the area of the triangle.
 - Sol. $\triangle ABC$ is an isosceles triangle in which AB = AC and $AD \perp BC$

Now, perimeter = 32 cm

$$andAD = 8 cm$$



Let
$$AB = AC = a$$

and
$$BC = b$$

$$\therefore BD = DC = \frac{b}{2}$$

Now, in right ΔABD,

$$AB^2 = BD^2 + AD^2$$

$$\Rightarrow a^2 = \frac{b^2}{4} + (8)^2$$

$$\Rightarrow 4a^2 = b^2 + 256$$

$$\Rightarrow 4a^2 - b^2 = 256$$

$$\Rightarrow (2a + b) (2a - b) = 256$$
 ...(i)

But,
$$AB + AC + BC = 32$$

$$\Rightarrow a + a + b = 32$$

$$\Rightarrow 2a + b = 32 \qquad ...(ii)$$

Dividing (i) by (ii),

$$2a - b = \frac{256}{32} = 8$$
 ...(iii)

Adding (ii) and (iii),

$$4a = 40$$

$$\Rightarrow a = 10$$

Subtracting (iii) from (ii),

$$2b = 24$$

$$\Rightarrow b = 12$$

Now, area of $\triangle ABC = \frac{BC \times AD}{2}$

$$=\frac{10\times12}{2}$$

$$= 60 \text{ cm}^2 \text{ Ans.}$$

- Q. 20. The area of a triangle is 216 cm² and its sides are in the ratio 3:4:5. Find the perimeter of the triangle.
 - Sol. Ratio in sides = 3:4:5

Let
$$AB = 3 x$$
, $BC = 4 x$

and
$$CA = 5x$$

$$\therefore s = \frac{AB + BC + CA}{2}$$

$$=\frac{3x+4x+5x}{2}$$

$$=\frac{12x}{2}=6x$$

:. Area of
$$\triangle ABC$$
,

$$= \sqrt{6x(6x-3x)(6x-4x)(6x-5x)}$$

$$= \sqrt{6x \times 3x \times 2x \times x}$$

$$= \sqrt{36x^4}$$

$$= 6x^2$$
But, area of triangle = 216 cm²

$$\therefore 6x^2 = 216$$

$$\Rightarrow x^2 = \frac{216}{6} = 36 = (6)^2$$

$$\therefore x = 6$$

:. Sides are
$$3 \times 6$$
, 4×6 , 5×6 or 18, 24, 30 cm.

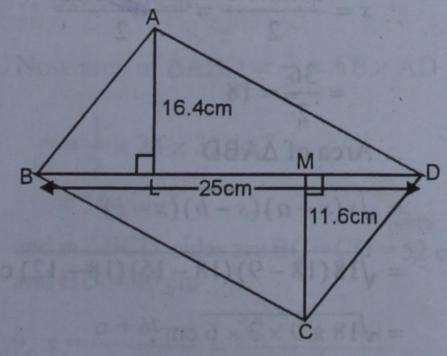
and perimeter = Sum of sides

$$= (18 + 24 + 30)$$
 cm

= 72 cm Ans.

EXERCISE 20 (B)

- Q. 1. Find the area of a quadrilateral one of whose diagonals is 25 cm long and the lengths of perpendiculars from the other two vertices one 16.4 cm and 11.6 cm respectively.
- Sol. In quadrilateral ABCD, diagonal BD = 25 cm



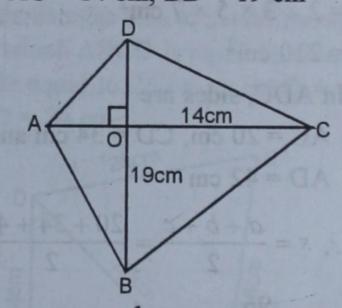
AL \perp BD and CM \perp BD AL = 16.4 cm, CM = 11.6

: Area of quadrilateral ABCD

$$=\frac{1}{2}(AL + CM) \times BD$$

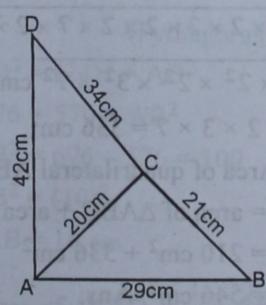
$$= \frac{1}{2}(16.4 + 11.6) \times 25 \,\mathrm{cm}^2$$
$$= \frac{1}{2} \times 28 \times 25 = 350 \,\mathrm{cm}^2 \,\mathrm{Ans.}$$

- Q. 2. The diagonals of a quadrilateral intersect each other at right angles. If the lengths of these diagonals be 14 cm and 19 cm respectively, find the area of the quadrilateral.
 - Sol. In quadrilateral ABCD,
 diagonals AC and BD intersect each
 other at O at right angles, and
 AC = 14 cm, BD = 19 cm



$$\therefore \text{ Area} = \frac{1}{2} \text{AC} \times \text{BD}$$
$$= \frac{1}{2} \times 14 \times 19 \text{ cm}^2 = 133 \text{ cm}^2 \text{ Ans.}$$

Q. 3. Find the area of a quadrilateral ABCD in which AB = 29 cm, BC = 21 cm, AC = 20 cm, CD = 34 cm and DA = 42 cm.



Sol. In quadrilateral ABCD, AC divides it into two triangles i.e. \triangle ABC and \triangle ADC. In \triangle ABC, sides are

$$AB = 29$$
 cm, $BC = 21$ cm and $AC = 20$ cm

$$\therefore s = \frac{a+b+c}{2}$$

$$= \frac{29+21+20}{2} = \frac{70}{2} = 35$$

:. Area of AABC

$$=\sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{35(35-29)(35-21)(35-20)}$$

$$= \sqrt{35 \times 6 \times 14 \times 15} \text{ cm}^2$$

$$= \sqrt{5 \times 7 \times 2 \times 3 \times 2 \times 7 \times 3 \times 5}$$

$$=\sqrt{2^2 \times 3^2 \times 5^2 \times 7^2}$$

$$= 2 \times 3 \times 5 \times 7 \text{ cm}^2$$

$$= 210 \text{ cm}^2$$

In ADC, sides are

$$AC = 20$$
 cm, $CD = 34$ cm and

$$AD = 42 \text{ cm}$$

$$\therefore s = \frac{a+b+c}{2} = \frac{20+34+42}{2}$$
$$= \frac{96}{2} = 48$$

:. Area of AADC

$$=\sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{48(48-20)(48-34)(48-42)} \text{ cm}^2$$

$$= \sqrt{48 \times 28 \times 14 \times 6} \text{ cm}^2$$

$$= \sqrt{2 \times 2 \times 2 \times 2 \times 3 \times 2 \times 2 \times 7 \times 2 \times 7 \times 2 \times 3}$$

$$= \sqrt{2^2 \times 2^2 \times 2^2 \times 2^2 \times 3^2 \times 7^2} \text{ cm}^2$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 7 = 336 \text{ cm}^2$$

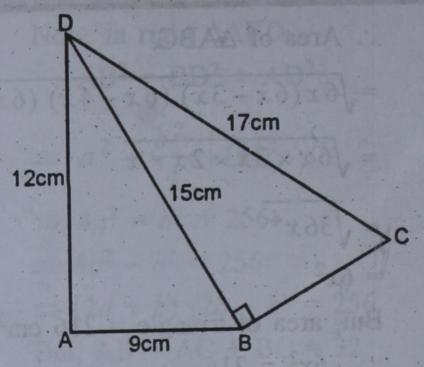
:. Area of quadrilateral ABCD

= area of $\triangle ABC$ + area of $\triangle ADC$

$$= 210 \text{ cm}^2 + 336 \text{ cm}^2$$

 $= 546 \text{ cm}^2 \text{ Ans.}$

Q. 4. Find the perimeter and area of quadrilateral ABCD in which AB = 9 cm, AD = 12 cm, BD = 15 cm, CD = 17 cm and ∠CBD = 90°.



Sol. In quadrilateral ABCD, diagonal BD divides it into two triangles.

In
$$\triangle BCD$$
, $\angle CBD = 90^{\circ}$

$$\therefore AC^2 = AB^2 + BC^2$$

(Pythagoras Theorem)

$$\Rightarrow (17)^2 = (15)^2 + BC^2$$

$$\Rightarrow 289 = 225 + BC^2$$

$$\Rightarrow$$
 BC² = 289 - 225 = 64 = (8)²

Now area of $\triangle DBC = \frac{1}{2} \times BC \times BD$

$$=\frac{1}{2} \times 8 \times 15 = 60 \text{ cm}^2$$

and in AABD, sides are

$$AB = 9 \text{ cm}$$
, $BD = 15 \text{ cm}$ and

$$AD = 12 \text{ cm}$$

$$\therefore s = \frac{a+b+c}{2} = \frac{9+15+12}{2}$$
$$= \frac{36}{2} = 18$$

: Area of AABD

$$=\sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{18(18-9)(18-15)(18-12)} \text{ cm}^2$$

$$= \sqrt{18 \times 9 \times 3 \times 6} \text{ cm}^2$$

$$= \sqrt{2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 2} \text{ cm}^2$$

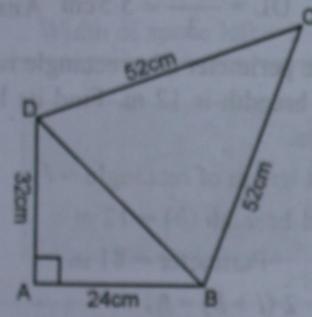
$$=\sqrt{2^2 \times 3^2 \times 3^2 \times 3^2}$$
 cm²

$$= 2 \times 3 \times 3 \times 3 = 54 \text{ cm}^2$$

- .. Area of quadrilateral ABCD
- = area of ΔDBC + area of ΔABD
- $= 60 \text{ cm}^2 + 54 \text{ cm}^2 = 114 \text{ cm}^2$

and perimeter = AB + BC + CD + DA

- $= (9 + 8 + 17 + 12) \text{ cm}^2$
- = 46 cm2 Ans.
- Q. 5. Calculate the area of quadrilateral ABCD in which: AB = 24 cm, AD = 32 cm, ∠BAD = 90° and BC = CD = 52 cm.



Sol. In quadrilateral ABCD, diagonal BD divides it into two triangles ΔABD and ΔBCD.

$$\therefore BD^2 = AD^2 + AB^2$$

(Pythagoras Theorem)

$$= (32)^2 + (24)^2 = 1024 + 576 = 1600$$
$$= (40)^2$$

Now area of $\triangle ABD = \frac{1}{2} \times AB \times AD$

$$=\frac{1}{2}\times24\times32\,\mathrm{cm}^2$$

 $= 384 \text{ cm}^2$

and in $\triangle BCD$, sides are BC = CD = 52 cm and BD = 40 cm

$$s = \frac{a+b+c}{2} = \frac{52+52+40}{2}$$
$$= \frac{144}{2} = 72$$

∴ Area of ∆BCD

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

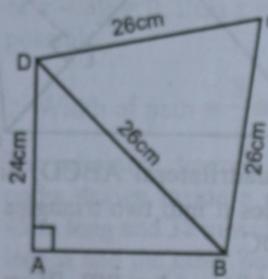
$$=\sqrt{72(72-52)(72-52)(72-40)}$$

$$= \sqrt{72 \times 20 \times 20 \times 32}$$

$$= \sqrt{2 \times 2 \times 2 \times 3 \times 3 \times 20 \times 20 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$= \sqrt{2^2 \times 2^2 \times 2^2 \times 2^2 \times 2^2 \times 3^2 \times 20^2} \text{ cm}^2$$

- $= 2 \times 2 \times 2 \times 2 \times 3 \times 20 \text{ cm}^2$
- $= 960 \text{ cm}^2$
- :. Area of quadrilateral ABCD
- = area of ΔABD + area of ΔBCD
- $=384 \text{ cm}^2 + 960 \text{ cm}^2$
- = 1344 cm2 Ans.
- Q. 6. Calculate the area of quadrilateral ABCD in which ΔBCD is equilateral with each side equal to 26 cm, ∠BAD = 90° and AD = 24 cm.



Sol. In quadrilateral ABCD, diagonal BD divides into two triangles : ΔABD and ΔBCD.

$$\therefore BD^2 = AD^2 + AB^2$$

(Pythagoras Theorem)

$$\Rightarrow (26)^2 = (24)^2 + AB^2$$

$$\Rightarrow 676 = 576 + AB^2$$

$$\Rightarrow$$
 AB² = 676 - 576 = 100

$$\Rightarrow$$
 AB² = (10)²

Now area of $\triangle ABD = \frac{1}{2} \times AB \times AD$

$$=\frac{1}{2}\times10\times24=120\,\mathrm{cm}^2$$

and area of equilateral ΔBCD whose each side is 26 cm

$$= \frac{\sqrt{3}}{4} (\text{side})^2 = \frac{1.732}{4} \times (26)^2 \text{ cm}^2$$

$$=\frac{1.732}{4}\times26\times26$$

$$= 0.433 \times 26 \times 26 \text{ cm}^2 = 292.71 \text{ cm}^2$$

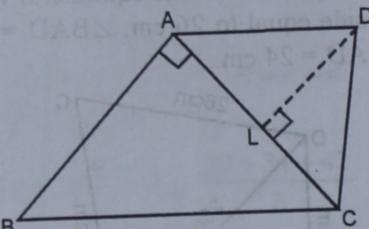
:. Area of quadrilateral ABCD

= area of $\triangle ABD$ + area of $\triangle BCD$

 $= 120 \text{ cm}^2 + 292.71 \text{ cm}^2$

 $= 412.71 \text{ cm}^2 \text{ Ans.}$

Q. 7. In the adjoining figure, $\triangle ABC$ is right angled at A, BC = 7.5 cm and AB = 4.5 cm. If the area of quadrilateral ABCD is 30 cm² and DL is the altitude of $\triangle DAC$, calculate the length DL.



Sol. In quadrilateral ABCD, diagonal AC divides it into two triangles ΔABC and ΔADC.

In $\triangle ABC$, $\angle A = 90^{\circ}$, BC = 7.5 cm and AB = 4.5 cm

But $BC^2 = AB^2 + AC^2$

(Pythagorus Theorem)

$$\Rightarrow (7.5)^2 = (4.5)^2 + AC^2$$

$$\Rightarrow 56.25 = 20.25 + AC^2$$

$$\Rightarrow$$
 AC² = 56.25 - 20.25

$$\Rightarrow AC^2 = 36 = (6)^2$$

 $\therefore \text{ Area of } \triangle ABC = \frac{1}{2} \times AB \times AC$

$$= \frac{1}{2} \times 4.5 \times 6 = 13.5 \,\mathrm{cm}^2$$

But area of quadrilateral ABCD

$$=30 \text{ cm}^2$$

$$\therefore$$
 Area of $\triangle ADC = 30 - 13.5$

 $= 16.5 \text{ cm}^2$

But area of AADC

$$= \frac{1}{2} \times \text{Base} \times \text{Altitude}$$

$$= \frac{1}{2} \times \text{AC} \times \text{DL}$$

$$= \frac{1}{2} \times 6 \times \text{DL} = 3 \text{DL}$$

$$\therefore 3 \cdot \text{DL} = 16.5$$

$$\Rightarrow \text{DL} = \frac{16.5}{3} = 5.5 \text{ cm Ans.}$$

- Q. 8. The perimeter of a rectangle is 81 m and its breadth is 12 m. Find its length and area.
- Sol. Let length of rectangle = l and breadth (b) = 12 m

Perimeter = 81 m

$$\therefore 2(l+b) = 81$$

$$2l+2b=81$$

$$\Rightarrow 2l + 2 \times 12 = 81$$

$$\Rightarrow 2l + 24 = 81$$

$$\Rightarrow 2l = 81 - 24 = 57$$

$$1 = \frac{57}{2} = 28.5 \,\mathrm{m}$$

Now area of the rectangle = $l \times b$

$$= 28.5 \times 12 \text{ m}^2 = 342.0 \text{ m}^2$$
. Ans.

- Q. 9. The perimeter of a rectangular field is $\frac{3}{5}$ km and its length is twice its breadth, find the area of the field in m².
 - Sol. Perimeter of rectangular field = $\frac{3}{5}$ km

$$=\frac{3}{5}\times1000=600\,\mathrm{m}$$

Let breadth of field = x m

then
$$length = 2x$$

$$2(2x+x) = 600$$

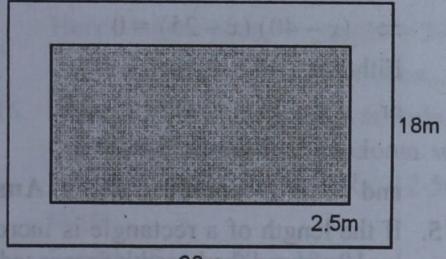
$$\Rightarrow$$
 6 x = 600

$$x = 100$$

:. Length =
$$2 x = 2 \times 100 = 200 \text{ m}$$

Breadth = $x = 100 \text{ m}$
Area = $l \times b = 200 \times 100$
= 20000 m^2 Ans.

- Q. 10. A rectangular plot 30 m long and 18 m wide is to be covered with grass leaving 2.5 m all around it. Find the area to be laid with grass.
 - Sol. Length of rectangular plot (l) = 30 mand width (b) = 18 mWidth of space left = 2.5 m



30m
:. Inner length
$$(l_1) = 30 - 2 \times 2.5$$

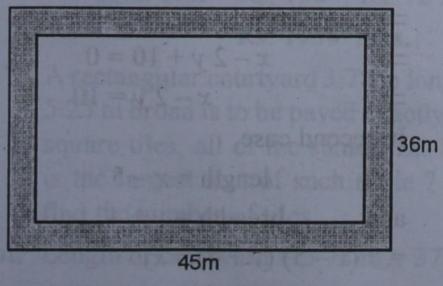
 $= 30 - 5 = 25 \text{ m}$

and Inner breadth
$$(b_1) = 18 - 2 \times 2.5$$

= 18 - 5 = 13 m

$$\therefore \text{ Area of grass area} = l_1 \times b_1$$
$$= 25 \text{ m} \times 13 \text{ m} = 325 \text{ m}^2 \text{ Ans.}$$

- Q. 11. A foot path of uniform width runs all around inside of a rectangular field 45 m long and 36 m wide. If the area of the path is 234 m², find the width of the path.
 - Sol. Length of field (l) = 45 mand breadth (b) = 36 mLet width of inner path = x



:. Inner length
$$(l_1) = 45 - 2 \times x$$

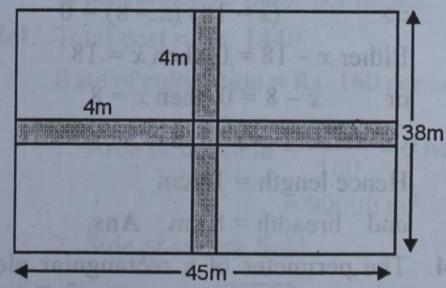
= $(45 - 2 x)$ m

and inner breadth
$$(b_1) = 36 - 2 \times x$$

 $= (36 - 2x)$ m
Area of path = 234 m²
 $\therefore l.b - l_1 b_1 = 234$
 $\Rightarrow 45 \times 36 - (45 - 2x) (36 - 2x) = 234$
 $1620 - (1620 - 90x - 72x + 4x^2) = 234$
 $\Rightarrow 1620 - (1620 - 162x + 4x^2) = 234$
 $\Rightarrow 1620 - 1620 + 162x - 4x^2 = 234$
 $\Rightarrow -4x^2 + 162x = 234$
 $\Rightarrow -4x^2 + 162x = 234$
 $\Rightarrow 2x^2 - 81x + 117 = 0$
 $\Rightarrow 2x^2 - 78x - 3x + 117 = 0$
 $\Rightarrow 2x(x - 39) - 3(x - 39) = 0$
Either $2x - 3 = 0$ then $x = \frac{3}{2}$
or $x - 39 = 0$, then $x = 39$ which is not possible.

:. Width of path =
$$\frac{3}{2}$$
 m = 1.5 m Ans.

Q. 12. The adjoining diagram shows two cross paths drawn inside a rectangular field 45 m long and 38 m wide, one parallel to length and the other parallel to breadth. The width of each path is 4 m. Find the cost of gravelling the paths at Rs. 5.60 per m².



$$\therefore \text{ Area of path} = l \times a + b \times a - a \times a$$

$$= (l+b) a - a^{2}$$

$$= (45 + 38) \times 4 - (4)^{2} \text{ m}^{2}$$

$$= 83 \times 4 - 16 = 332 - 16 = 316 \text{ m}^{2}$$

Rate of gravelling the path

= Rs. 5.60 per m²

Total cost = Rs. 316 × 5.60

= Rs. 1769.60 Ans.

- Q. 13. A rectangle of area 144 cm² has its length equal to x cm. Write down its breadth in terms of x. Given that its perimeter is 52 cm, write down an equation in x and solve it to determine the dimensions of the rectangle.
 - Sol. Area of rectangle = 144 cm²
 Perimeter = 52 cm

Length of rectangle = x

∴ Breadth =
$$\frac{\text{Area}}{\text{Length}} = \frac{144}{x} \text{cm}$$

or Breadth = $\frac{\text{Perimeter} - 2 \text{ Length}}{2}$
= $\frac{52 - 2x}{2} = (26 - x) \text{ cm}$

Now Area = length \times breadth

$$\Rightarrow 144 = x \times (26 - x)$$

$$\Rightarrow 144 = 26 x - x^2$$

$$\Rightarrow x^2 - 26x + 144 = 0$$

$$\Rightarrow x^2 - 18 x - x + 144 = 0$$

$$\therefore x(x-18)-8(x-18)=0$$

$$\Rightarrow (x-18)(x-8)=0$$

Either
$$x - 18 = 0$$
, then $x = 18$

or
$$x - 8 = 0$$
, then $x = 8$

$$x = 18, 8$$

Hence length = 18 cm

and breadth = 8 cm Ans.

Q. 14. The perimeter of a rectangular plot is 130 m and its area is 1000 m². Take the length of the plot as x metres. Use the perimeter to write the value of breadth in terms of x. Use the values of length, breadth and area to write an equation in x. Solve the equation and calculate the length and breadth of the plot.

Sol. Area of rectangular field = 1000 m^2 and perimeter = 130 mLet length of the field = x m

:. Breadth =
$$\frac{130 - 2x}{2} = (65 - x)m$$

$$\therefore$$
 Area = $l \times b$

$$\Rightarrow 1000 = x (65 - x)$$

$$\Rightarrow 1000 = 65 x - x^2$$

$$\therefore x^2 - 65 x + 1000 = 0$$

$$\Rightarrow x^2 - 40 x - 25 x + 1000 = 0$$

$$\Rightarrow x(x-40) - 25(x-40) = 0$$

$$\Rightarrow$$
 $(x-40)(x-25)=0$

Either x - 40 = 0, then x = 40

or
$$x - 25 = 0$$
, then $x = 25$

:. Length of the field = 40 m

and breadth = 25 m Ans.

- Q. 15. If the length of a rectangle is increased by 10 cm and the breadth decreased by 5 cm, the area remains unchanged. If the length is decreased by 5 cm and the breadth is increased by 4 cm, even then the area remains unchanged. Find the dimensions of the rectangle.
 - Sol. Let length of a rectangle = x cm and breadth = y cm and area = $l \times b = xy$ cm² In first case

length =
$$(x + 10)$$
 cm

and breadth =
$$(y-5)$$
 cm.

$$(x+10)(y-5) = xy$$

$$\Rightarrow xy - 5x + 10y - 50 = xy$$

$$\Rightarrow -5x + 10y - 50 = 0$$

$$\Rightarrow x - 2y + 10 = 0$$

$$x - 2y = 10$$

...(ii)

In second case,

length =
$$x - 5$$

and breadth =
$$y + 4$$

$$(x-5)(y+4) = xy$$

$$\Rightarrow xy + 4x - 5y - 20 = xy$$

$$\Rightarrow 4x - 5y = 20$$

$$5x - 10y = -50$$

 $8x - 10y = 40$

Subtracting,
$$-3x = -90 \implies x = 30$$

Substituting the value of x in (i)

$$30 - 2y = -10$$

$$\Rightarrow -2y = -10 - 30 = -40$$

$$\therefore y = \frac{-40}{-2} = 20$$

Hence length of the rectangle = 30 cm and breadth = 20 cm Ans.

- Q. 16. A room is 13 m long and 9 m wide. Find the cost of carpeting the room with a carpet 75 cm wide and Rs. 12.50 per metre.
 - Sol. Length of room (l) = 13 mand width (b) = 9 m
 - $\therefore \text{ Area of the floor} = l \times b$ $= 13 \text{ m} \times 9 \text{ m}$ $= 117 \text{ m}^2$

Width of carpet = 75 cm = $\frac{75}{100} = \frac{3}{4}$ m

: Length of carpet = Area ÷ Width

$$= 117 \div \frac{3}{4} = \frac{117 \times 4}{3} \text{ m}$$
$$= 156 \text{ m}$$

Rate of carpet = Rs. 12.50 per m

$$\therefore \text{ Total cost} = \text{Rs. } 156 \times \text{Rs. } 12.50$$
$$= \text{Rs. } 1950 \text{ Ans.}$$

- Q. 17. A rectangular courtyard 3.78 m long and 5.25 m broad is to be paved exactly with square tiles, all of the same size. What is the largest size of such a tile? Also find the number of tiles.
 - Sol. Length of courtyard = 3.78 m = 378 cm Width of courtyard = 5.25 m = 525 cm ∴ Largest size of the square tile used

Area of the courtyard = $l \times b$ = 378 × 525 cm²

Area of one tile = $21 \times 21 \text{ cm}^2$

: No. of tiles

$$= \frac{378 \times 525}{21 \times 21} = 18 \times 25$$
$$= 450$$

- Q. 18. The cost of cultivating a square field at the rate of 160 per hectare is Rs. 1440. Find the cost of putting fence around it at the rate of 75 paise per metre.
 - Sol. Total cost = Rs. 1440

Rate of cultivation = Rs. 160 per hectare

$$\therefore \text{ Area of the field} = \frac{1440}{160} = 9 \text{ hectare}$$
$$= 90000 \text{ m}^2$$

: Side of square field

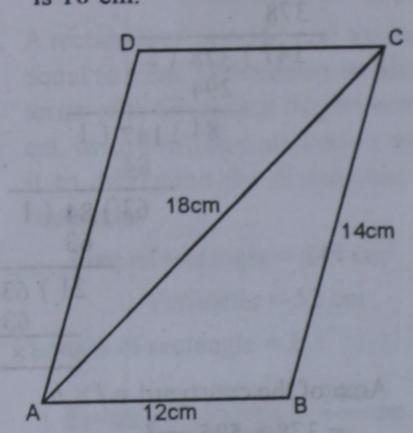
$$=\sqrt{90000} = 300 \text{ m}$$

and perimeter of the square field = 4a= $4 \times 300 = 1200 \text{ m}$

Rate of fencing = 75 paise per metre

$$\therefore \text{ Total cost} = \text{Rs.} \frac{1200 \times 75}{100}$$
$$= \text{Rs.} 900 \text{ Ans.}$$

Q. 19. Find the area of a parallelogram, if its two adjacent sides are 12 cm and 14 cm and if the diagonal connecting their ends is 18 cm.



Sol. : Diagonals bisect the parallelogram into two triangle of equal area.

:. Area of parallelogram ABCD = 2 area of \triangle ABC

Now sides of ΔABC are 12 cm, 14 cm, 18 cm

$$s = \frac{a+b+c}{2} = \frac{12+14+18}{2}$$
$$= \frac{44}{2} = 22$$

and Area of AABC

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{22(22-12)(22-14)(22-18)}$$

$$= \sqrt{22 \times 10 \times 8 \times 4}$$

$$= \sqrt{11 \times 2 \times 2 \times 5 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$=\sqrt{2^2 \times 2^2 \times 2^2 \times 110}$$

$$= 2 \times 2 \times 2\sqrt{110} = 8\sqrt{110} \text{ cm}^2$$

:. Area of parallelogram ABCD

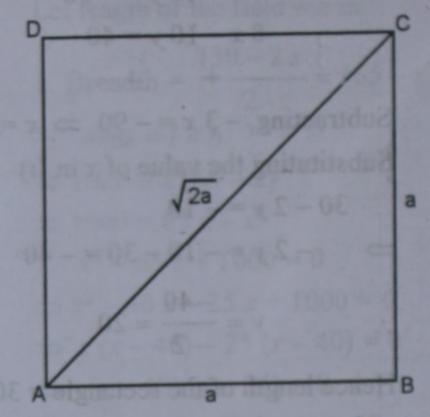
= $2 \times \text{area of } \Delta ABC$

$$= 2 \times 8\sqrt{110} = 16\sqrt{110} \text{ cm}^2$$

$$= 16 \times 10.488 = 167.81 \text{ cm}^2$$

 $= 167.8 \text{ cm}^2 \text{ Ans.}$

Q. 20. Find the length of the diagonal of a square of area 200 cm².



Sol. Let side of square
$$= a$$

Area =
$$a^2$$

and length of diagonal = $\sqrt{2} a$

$$= \sqrt{2 a^2}$$

$$= \sqrt{2 \times \text{Area}}$$

$$= \sqrt{2 \times 200} = \sqrt{400} = 20 \text{ cm Ans.}$$

Q. 21. The area of a square field is 8 hectares.

How long would a man take to cross it diagonally by walking at the rate of 4 kmph?

: Length of its diagonal = $\sqrt{2} \times \text{area}$

$$= \sqrt{2 \times 80000} \text{ m} = \sqrt{160000} = 400 \text{ m}$$

Speed of a man = 4 kmph

:. Time taken by him

$$= \frac{400 \times 1}{40 \times 1000} = \frac{1}{10} \text{ hour}$$

$$= \frac{1}{10} \times 60 = 6 \text{ minutes Ans.}$$

Q. 22. Find the area and perimeter of a square plot of land whose diagonal is 15 m. Give your answer correct to two decimal places.

Sol. Diagonal of a square plot = 15 m

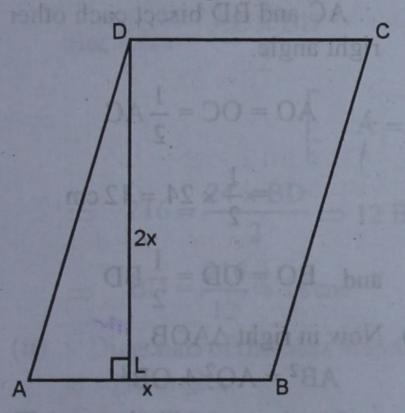
$$\therefore \text{ Its side} = \frac{\text{Diagonal}}{\sqrt{2}} = \frac{15}{\sqrt{2}} \,\text{m}$$

(i) Area =
$$(\text{side})^2 = \left(\frac{15}{\sqrt{2}}\right)^2$$

= $\frac{225}{2} = 112.5 \,\text{m}^2$

(ii) and perimeter =
$$4a = \frac{4 \times 15}{\sqrt{2}} = \frac{60}{\sqrt{2}}$$
 m
= $\frac{60 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{60\sqrt{2}}{2} = 30\sqrt{2}$ m
= $30 (1.414) = 42.42$ m Ans.

- Q. 23. The area of a parallelogram is 338 m². If its altitude is twice the corresponding base, determine the base and the altitude.
 - Sol. Area of parallelogram = 338 m^2 Let base of the parallelogram = x m



$$\therefore$$
 Altitude = 2 x

and Area = Base × Altitude
=
$$x \times 2 x = 2 x^2$$

$$2x^2 = 338$$

$$\Rightarrow x^2 = \frac{338}{2} = 169 = (13)^2$$

(ii) Now area of the
$$EI = x \setminus BCD$$
:

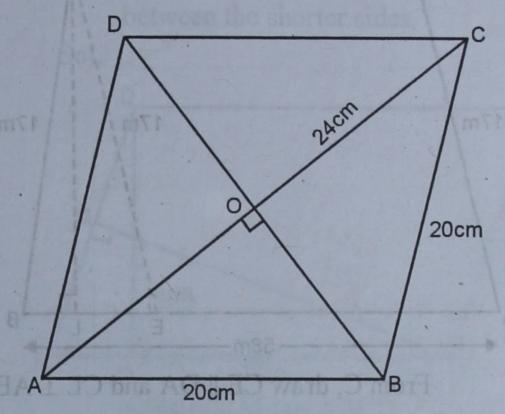
$$\therefore \quad \text{Base} = x = 13 \text{ m and}$$

$$\text{altitude} = 2 x = 2 \times 13 \text{ m}$$

$$= 26 \text{ m Ans.}$$

- Q. 24. Find the area of a rhombus one side of which measures 20 cm and one of whose diagonals is 24 cm.
 - Sol. In rhombus ABCD,

each side =
$$20 \text{ cm}$$
 and one diagonal AC = 24 cm



- The diagonals of a rhombus bisect each other at right angles.
- .. AC and BD bisect each other at O at right angle.

Hence AOB is a right triangle in which AB = 20 cm,

$$AO = \frac{1}{2}AC = \frac{1}{2} \times 24 = 12 \text{ cm}$$

But
$$AB^2 = AO^2 + OB^2$$

$$\Rightarrow (20)^2 = (12)^2 + OB^2$$

$$\Rightarrow$$
 400 = 144 + OB²

$$\Rightarrow$$
 OB² = 400 - 144 = 256 = (16)²

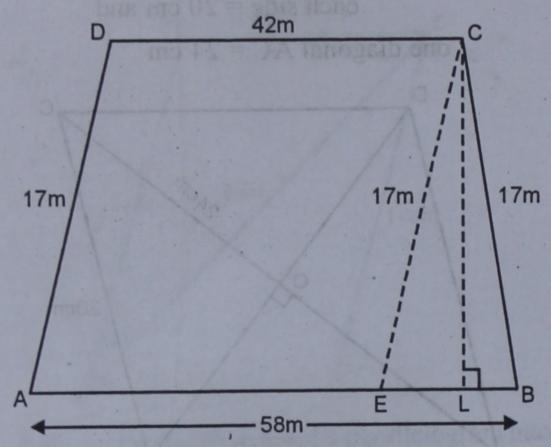
$$\therefore \text{ Diagonal BD} = 2 \times \text{OB}$$
$$= 2 \times 16 = 32 \text{ cm}$$

Now area of rhombus

$$= \frac{\text{Product of diagonals}}{2}$$
$$= \frac{24 \times 32}{2} = 384 \,\text{cm}^2 \text{ Ans.}$$

Q. 25. The two parallel sides of a trapezium are 58 m and 42 m long. The other two sides are equal, each being 17 m. Find its area.

Sol. In trapezium ABCD



From C, draw CE || DA and CL \(\perp \) AB meeting AB in E such that

$$AE = CD = 42 \text{ m}$$
 and $EB = AB - AE$

$$\Rightarrow EB = 58 - 42 = 16 \text{ m}$$

$$CE = DA = 17 \text{ m}$$

.. ΔECB is an isosceles triangle and CL \(\pm\)EB

:. CL bisects EB at L

:.
$$EL = \frac{1}{2}EB = \frac{1}{2} \times 16 = 8 \text{ m}$$

Now in right $\triangle CEL$,

$$CE^2 = CL^2 + EL^2$$

(Pythagoras Theorem)

$$\Rightarrow (17)^2 = CL^2 + (8)^2$$

$$\Rightarrow 289 = CL^2 + 64$$

$$\Rightarrow$$
 CL² = 289 - 64 = 225 = (15)²

Now area of trapezium ABCD

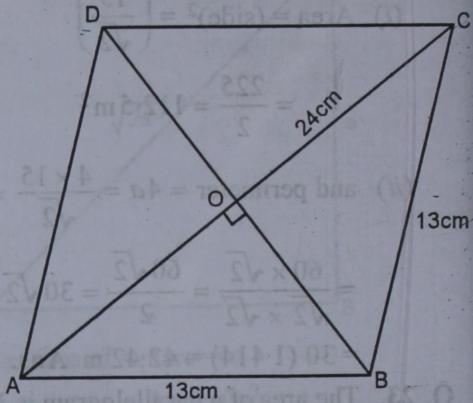
$$= \frac{1}{2} (AB + CD) \times CL$$

$$= \frac{1}{2} (58 + 42) \times 15 \text{ m}^2$$

$$= \frac{1}{2} \times 100 \times 15 \text{ m}^2 = 750 \text{ m}^2 \text{ Ans.}$$

- Q. 26. The perimeter of a rhombus is 52 cm. If one of its diagonals is 24 cm long, find:
 - (i) The length of other diagonal.
 - (ii) The area of the rhombus.

Sol.



Side AB of the rhombus ABCD = 13 cm and diagonal AC = 24 cm

- : Diagonals of a rhombus bisect each other at right angles.
- : AC and BD bisect each other at O at right angle.

$$AO = OC = \frac{1}{2}AC$$

$$= \frac{1}{2} \times 24 = 12 \text{ cm}$$

and
$$BO = OD = \frac{1}{2}BD$$

(i) Now in right $\triangle AOB$,

$$AB^2 = AO^2 + OB^2$$

(Pythagoras Theorem)

$$\Rightarrow$$
 (13)² = (12)² + OB²

$$\Rightarrow 169 = 144 + OB^2$$

$$\Rightarrow$$
 OB² = 169 - 144 = 25 = (5)²

$$\therefore$$
 OB = 5 cm

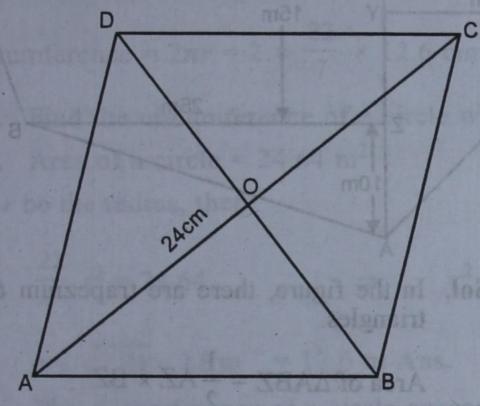
:.
$$BD = 2 OB = 2 \times 5 = 10 cm$$

(ii) Now area of rhombus ABCD

$$= \frac{\text{Product of diagonals}}{2} = \frac{\text{AC} \times \text{BD}}{2}$$

$$=\frac{24\times10}{2}=120\,\mathrm{cm}^2$$
 Ans.

- Q. 27. The area of a rhombus is 216 cm² and one of its diagonals measures 24 cm. Find:
 - (i) The length of other diagonal.
 - (ii) The length of each of its sides.
 - (iii) Its perimeter.



Sol. (i) Area of rhombus ABCD = 216 cm^2 one diagonal AC = 24 cm

But Area =
$$\frac{AC \times BD}{2}$$

$$\left[:: A = \frac{d_1 \times d_2}{2} \right]$$

$$\Rightarrow 216 = \frac{24 \times BD}{2} \Rightarrow 12 BD = 216$$

$$\Rightarrow BD = \frac{216}{12} = 18 \text{ cm}$$

- (ii) : Diagonals of rhombus bisect each other at right angles.
 - :. AC and BD bisect at O at right angles.

$$\therefore AO = OC = \frac{1}{2}AC$$

$$= \frac{1}{2} \times 24 = 12 \text{ cm}$$

BO = OD =
$$\frac{1}{2}$$
 BD = $\frac{1}{2} \times 18 = 9$ cm

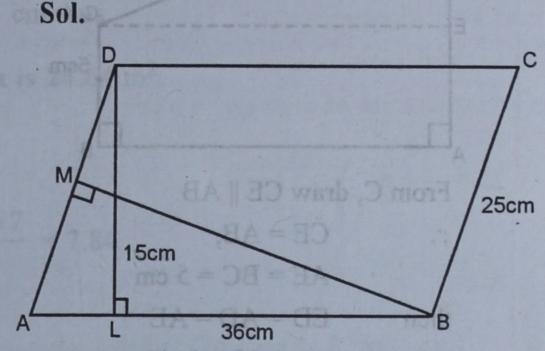
Now in right $\triangle AOB$,

$$AB^2 = AO^2 + OB^2 = (12)^2 + (9)^2$$

= 144 + 81 = 225 = (15)²

Hence each side of the rhombus = 15 cm.

- (iii) Perimeter of rhombus = $4 \times \text{side}$ = $4 \times 15 = 60 \text{ cm Ans.}$
- Q. 28. Two adjacent sides of a parallelogram are 36 cm and 25 cm. If the distance between longer sides is 15 cm, find the distance between the shorter sides.



In parallelogram ABCD,

$$AB = 36 \text{ cm}, BC = 25 \text{ cm}$$

Now area of parallelogram ABCD

$$=$$
 Base \times Altitude $=$ AB \times DL

$$= 36 \times 15 = 540 \text{ cm}^2$$

Again area of parallelogram ABCD

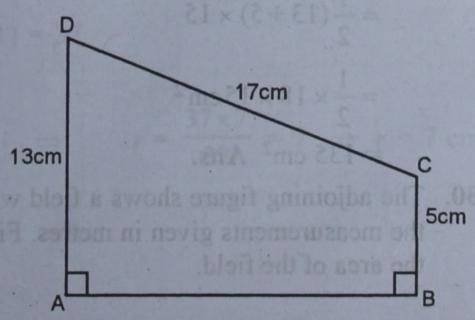
$$= AD \times BM$$

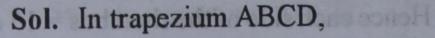
$$\Rightarrow$$
 540 = 25 × BM

$$\Rightarrow BM = \frac{540}{25}$$

BM =
$$21.6$$
 cm Ans.

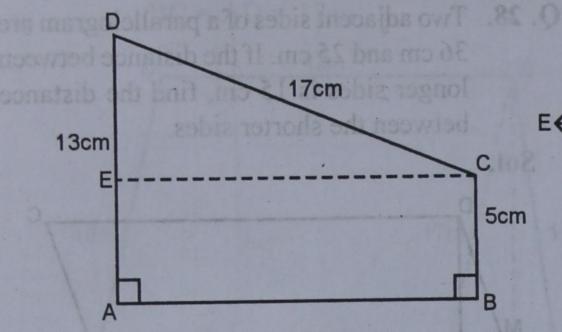
Q. 29. In the given figure, ABCD is a trapezium in which AD = 13 cm, BC = 5 cm, CD = 17 cm and ∠A = ∠B = 90°. Calculate: (i) AB (ii) Area of trap. ABCD.





$$AD = 13 \text{ cm}, BC = 5 \text{ cm}, CD = 17 \text{ cm}$$

$$\angle A = \angle B = 90^{\circ}$$



From C, draw CE | AB

$$\therefore$$
 CE = AB,

$$AE = BC = 5 \text{ cm}$$

then
$$ED = AD - AE$$

= $13 - 5 = 8$ cm

(i) Now in right ΔDEC,

$$CD^2 = DE^2 + EC^2$$

(Pythagoras Theorem)

$$\Rightarrow (17)^2 = (8)^2 + EC^2$$

$$\Rightarrow 289 = 64 + EC^2$$

$$\Rightarrow$$
 EC² = 289 - 64

$$\Rightarrow EC^2 = 225 = (15)^2$$

But
$$AB = EC$$
 : $AB = 15$ cm

(ii) Now area of trapezium ABCD

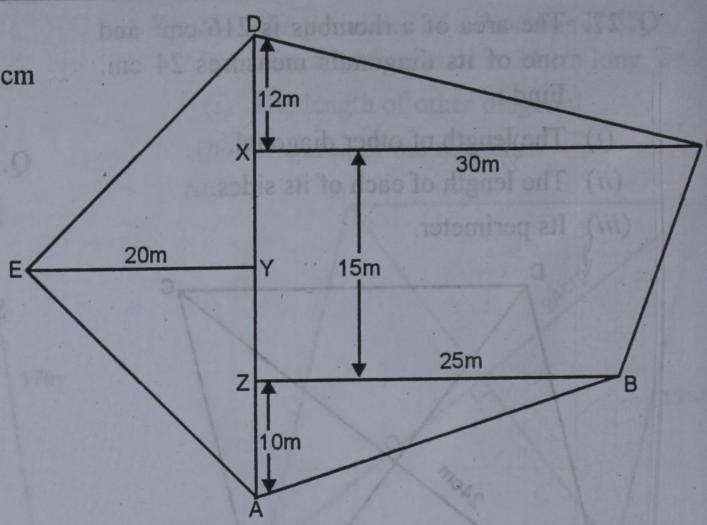
$$= \frac{1}{2}(AD + BC) \times AB$$

$$= \frac{1}{2}(13 + 5) \times 15$$

$$= \frac{1}{2} \times 18 \times 15 \text{ cm}^2$$

$$= 135 \text{ cm}^2 \text{ Ans.}$$

Q. 30. The adjoining figure shows a field with the measurements given in metres. Find the area of the field.



Sol. In the figure, there are trapezium and triangles.

Area of
$$\triangle ABZ = \frac{1}{2}AZ \times BZ$$

$$= \frac{1}{2} \times 10 \times 25 = 125 \,\mathrm{m}^2$$

Area of trapezium BZXC

$$= \frac{1}{2}(BZ + XC) \times ZX$$

$$=\frac{1}{2}(25+30)\times15\,\mathrm{m}^2$$

$$= \frac{1}{2} \times 55 \times 15 \,\mathrm{m}^2 = \frac{825}{2} = 412.5 \,\mathrm{m}^2$$

Area of
$$\Delta XCD = \frac{1}{2}CX \times DX$$

$$= \frac{1}{2} \times 30 \times 12 = 180 \text{ m}^2$$

and area of
$$\triangle AED = \frac{1}{2} \times AD \times EY$$

$$= \frac{1}{2}(10 + 15 + 12) \times 20 \,\mathrm{m}^2$$

$$= \frac{1}{2} \times 37 \times 20 = 370 \,\mathrm{m}^2$$

 \therefore Area of ABCDE = area of \triangle ABZ

+ area of BZXC + area of ΔXCD

+ area of \triangle AED

$$= 125 + 412.5 + 180 + 370 \text{ m}^2$$

 $= 1087.5 \text{ m}^2 \text{ Ans.}$

EXERCISE 20 (C)

1. Find the area and circumference of the circle whose radius is 12.6 cm.

Sol. Radius
$$(r) = 12.6$$
 cm

$$\therefore \text{ Area} = \pi r^2 = \frac{22}{7} \times (12.6)^2 \text{ cm}^2 = \frac{22}{7} \times 12.6 \times 12.6 \text{ cm}^2 = 498.96 \text{ cm}^2$$

Circumference = $2\pi r = 2 \times \frac{22}{7} \times 12.6 \text{ cm}^2 = 79.2 \text{ cm Ans.}$

2. Find the circumference of a circle whose area is 24.64 m².

Sol. Area of a circle = 24.64 m²

Let r be the radius, then

Let r be the radius, then
$$\Rightarrow \frac{22}{7} r^2 = 24.64 \Rightarrow r^2 = \frac{24.64 \times 7}{22} = 7.84$$

$$r = \sqrt{7.84} = 2.8 \,\text{m} = 17.6 \,\text{m} \,\text{Ans.}$$

The circumference of a circle exceeds its diameter by 42 cm. Find the area of the circle.

Sol. Let r be the radius of the circle

$$\therefore \text{ Diameter} = 2r$$

and C = 2r + 42

$$\Rightarrow 2\pi r = 2r + 42 \Rightarrow \frac{2 \times 22}{7} r - 2r = 42$$

$$\Rightarrow \frac{44r - 14r}{7} = 42 \qquad \Rightarrow \frac{30r}{7} = 42 \qquad \Rightarrow r = \frac{42 \times 7}{30} = \frac{49}{5} \text{ cm}$$

Area =
$$\pi r^2 = \frac{22}{7} \times \frac{49}{3} \times \frac{49}{3} = \frac{7446}{25} = 301.84 \text{ cm}^2 \text{ Ans.}$$

4. The difference between the circumference and the radius of a circle is 37 cm. Find the area of the circle.

cm and breadth BC = 14 cm

Sol. Let r be the radius

$$\therefore C-r=37$$

$$\Rightarrow 2\pi r - r = 37 \qquad \Rightarrow \qquad r\left(2 \times \frac{22}{7} - 1\right) = 37$$

$$\Rightarrow r\left(\frac{44-7}{7}\right) = 37 \qquad \Rightarrow \qquad r \times \frac{37}{7} = 37 \qquad \Rightarrow \qquad r = \frac{37\times7}{37} = 7 \Rightarrow r = 7 \text{ cm}$$

Now area =
$$\pi r^2 = \frac{22}{7} \times 7 \times 7$$

5. Between a square of perimeter 44 cm a circle of circumference 44 cm, which figure has larger area and by how much?

Sol. In first case,

Perimeter of a square = 44 cm

$$\therefore \text{ Side} = \frac{44}{4} = 11 \text{ cm}$$

and area = $(side)^2 = 11 \times 11 = 121 \text{ cm}^2$

In second case,

Circumference of a circle = 44 cm

$$\therefore 2\pi r = 44 \Rightarrow \frac{2 \times 22}{7} r = 44 \Rightarrow r = \frac{44 \times 7}{44} = 7 \text{ cm}$$

:. Area =
$$\pi r^2 = \frac{22}{7} \times 7 \times 7 = 154 \text{ cm}^2$$

It is clear that area of circle is greater

- :. Difference = $154 121 = 33 \text{ cm}^2 \text{ Ans.}$
- Q. 6. The circumference and the area of a circle are numerically equal. Find the diameter of the circle drawn inside a rectangle with sides 18 cm and 14 cm?

Sol. Let radius of the circle = r

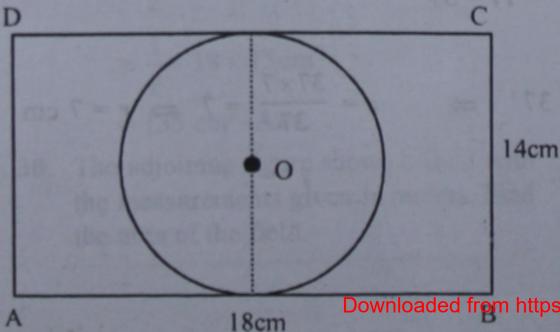
- : circumference = $2\pi r$ and area = πr^2
- . The circumference and area of a circle a equal

$$\therefore 2\pi r = \pi r^2 \implies 2 = r$$

- \therefore Diameter = $2r = 2 \times 2 = 4$ units Ans.
- 7. Find the area of the largest circle that can be drawn inside a rectangle with sides 18 cm and 14 cm.
- Sol. ABCD is rectangle whose length AB = 18 cm and breadth BC = 14 cm

A largest circle can be drawn

with diameter 14 cm in the rectangle



 $\therefore \text{ Radius } (r) = \frac{14}{2} = 7 \text{ cm}$

Now area =
$$\pi r^2 = \frac{22}{7} \times 7 \times 7 \text{ cm}^2$$

= 154 cm² Ans.

- 8. A circular wire of radius 56 cm is bent in the form of a square. Find the area of the square formed.
- Sol. Radius of the circular wire (r) = 56 cm
 - $\therefore \text{ Circumference} = 2\pi r$

$$= 2 \times \frac{22}{7} \times 56 = 352 \text{ cm}$$

Now perimeter of square wire formed by the circular wire = 352 cm

:. Side =
$$\frac{352}{4}$$
 = 88 cm

Area of the square = $a^2 = (85)^2 \text{ cm}^2$ = 7744 cm² Ans.

- 9. A wire can be bent in form of a circle of radius 42 cm. If it is bent in the form of a rectangle whose sides are in the ratio 6: 5, find the area of the rectangle formed.
- Sol. Radius of the circular wire = 42 cm
 - \therefore Circumference = $2\pi r$

$$= 2 \times \frac{22}{7} \times 42 = 264$$
 cm

Now perimeter of the rectangle formed by the circular wire = 264 cm

$$\Rightarrow$$
 2(l+b) = 264

$$\Rightarrow l+b=\frac{264}{2}=132$$

But ratio in l:b=6:5

:. Length (1) =
$$\frac{132 \times 6}{6+5} = \frac{132 \times 6}{11} = 72 \text{ cm}$$

and width (b) =
$$\frac{132 \times 5}{11}$$
 = 60 cm

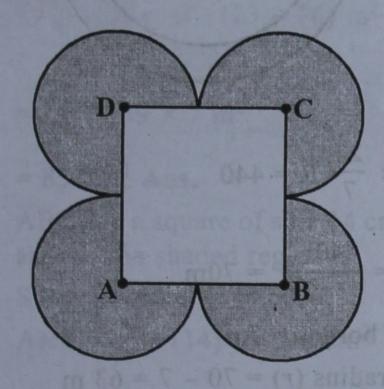
 \therefore Area of the rectangle = $l \times b$

- 10. A square tank has an area of 1764 m². There are four semicircular plots arround it. Find the cost of turfing the plots at Rs. 15 per m².
- **Sol.** Area of the square $tank = 1764 \text{ m}^2$

$$\therefore \text{ Side} = \sqrt{\text{Area}} = \sqrt{1764} \text{ m} = 42 \text{ m}$$

Now diameter of each semicircular lower plots on its sides = 42 m

:. Radius $(r) = \frac{42}{2} = 21 \text{ m}$



 $\therefore \text{Area of four semicular plots} = 4 \times \frac{1}{2} \pi r^2$

$$= 2 \times \frac{22}{7} \times 21 \times 21 \text{ m}^2 = 2772 \text{ m}^2$$

Rate of turfing = Rs. 15 per m²

- $\therefore \text{ Total cost} = \text{Rs. } 15 \times 2772$ = Rs. 41580 Ans.
- 11. The cost of fencing a circular field at Rs. 11.50 per metre is Rs. 2530. The field is to be ploughed at the rate of Rs. 6.50 per m². Find the cost of ploughing the field.
- Sol. Cost of fencing the circular field

Rate of fencing = Rs. 11.50 per metre

$$\therefore \text{ Circumference of the field} = \frac{2530}{11.50}$$

$$= \frac{2530}{11.50} \times 100 \text{m} = \frac{2530 \times 100}{1150} \text{m}$$

$$= 220 \text{ m}$$

Let r be the radius of the field

$$\therefore 2\pi r = 220$$

$$\Rightarrow \frac{2 \times 22}{7} r = 220$$

$$\Rightarrow r = \frac{220 \times 7}{2 \times 22} = 35 \text{ m}$$

and area of the field = πr^2

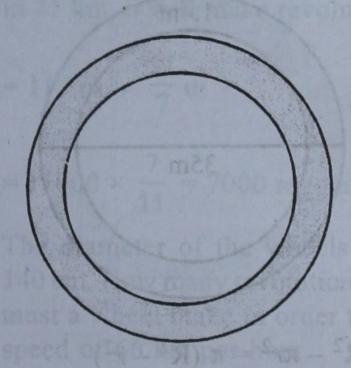
Area of the field = πr^2

$$= \frac{22}{7} \times 35 \times 35 \text{ m}^2.$$

$$= 3850 \text{ m}^2$$

Rate of ploughing the field = Rs. 6.50 per m

- .. Total cost = Rs. 3850×6.50 = Rs. 25025 Ans.
- 12. The areas of two concentric circles forming or ring are 154 cm² and 616 cm². Find the width of the ring.



Sol. Area of outer circle = 616 cm²

$$\therefore \text{ Outer radius} = \sqrt{\frac{\text{Area}}{\pi}}$$

$$= \sqrt{\frac{616 \times 7}{22}} \text{ cm}$$

$$=\sqrt{196} = 14 \text{ cm}$$

Area of inner circle = 154 cm²

$$\therefore \text{ Inner radius} = \sqrt{\frac{\text{Area}}{\pi}}$$

$$= \sqrt{\frac{154 \times 7}{22}} \text{ cm}$$

$$=\sqrt{49} = 7 \text{ cm}$$

- ... Width of the ring so formed = 14 7 = 7 cm Ans.
- 13. A circular ground whose diameter is 35 metres has a 1.4 m broad garden around it. What is the area of the garden is square meters.
- Sol. Diameter of the circular ground = 35 m

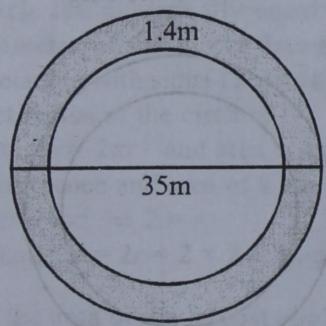
$$\therefore \text{ Radius (R)} = \frac{35}{2} \text{ m}$$

Width of garden around it = 1.4 cm

:. Inner radius =
$$(r)$$

= $(17.5 - 1.4)$ m
= 16.1 m

Now, area of the garden



$$= \pi R^2 - \pi r^2 = \pi (R^2 - r^2)$$

$$= \pi (R + r) (R - r)$$

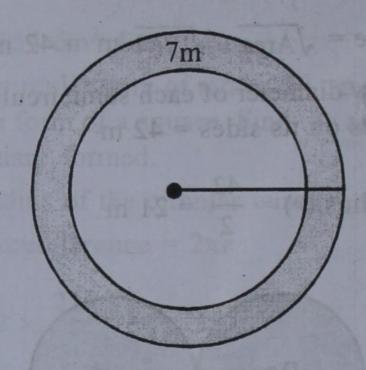
$$= \frac{22}{7} [17.5 + 16.1] [17.5 - 16.1]$$

$$= \frac{22}{7} \times 33.6 \times 1.4 \text{ m}^2$$

$$= 147.84 \text{ m}^2 \text{ Ans.}$$

14. A circular garden has circumference of 440 m. There is a 7 m wide border inside the garden along its periphery. Find the area of the border.

Sol. Width of border = 7cm Circumference of the garden = 440 m Let R be the radius of the garden Then $2\pi R = 440$



$$\Rightarrow 2 \times \frac{22}{7} R = 440$$

$$\Rightarrow R = \frac{440 \times 7}{2 \times 22} = 70m$$

Width of border = 7m

:. Inner radius
$$(r) = 70 - 7 = 63 \text{ m}$$

Now area of border =
$$\pi [R^2 - r^2]$$

$$=\pi (R+r) (R-r)$$

$$=\frac{22}{7}(70+63)(70-63)$$

$$=\frac{22}{7}\times 133\times 7~\text{m}^2$$

$$= 2926 \text{ m}^2 \text{ Ans.}$$

- 15. A rope by which a cow is tethered is increased from 16m to 23 m. How much additional ground does it have now to graze?
- Sol. Let length of rope in first case (r)

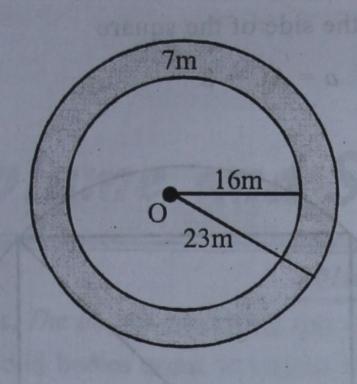
$$r = 16 \text{ m}$$

and by increasing it R = 23 m

.. Area of additional ground to be grazed

$$=\pi(\mathbf{R}^2-r^2)$$

$$=\frac{22}{7} (23^2 - 16^2) \text{ m}^2$$



$$= \frac{22}{7} (23 + 16) (23 - 16) m^{2}$$

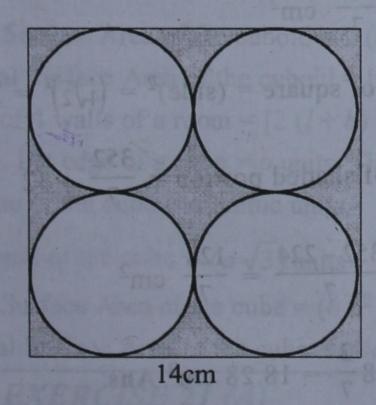
$$= \frac{22}{7} \times 39 \times 7 m^{2}$$

$$= 858 m^{2} Ans.$$

- 16. ABCD is a square of side 14 cm. Find the area of the shaded region.
- Sol. Side of square = 14 cm

:. Area =
$$a^2$$
 = $(14)^2$ = 196 cm²

Diameter of each circle drawn in it = $\frac{14}{2}$ = 7 cm



$$\therefore \text{ Radius } (r) = \frac{7}{2} \text{ cm}$$
Now area of each circle = πr^2

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \text{ cm}^2$$

$$=\frac{77}{2} \text{ cm}^2$$

and area of 4 circle = $\frac{77}{2}$ × 4 = 154 cm²

- :. Area of shaded portion = (196 154) cm² = 42 cm² Ans.
- 17. The radius of a wheel is 0.25 m. Find the number of revolutions it will make travel a distance of 11 km.
- **Sol.** Radius of wheel (r) = 0.25 m
 - $\therefore \text{ Circumference} = 2\pi r$

$$=2\times\frac{22}{7}\times0.25$$

$$= \frac{11}{7} \text{ m and to leady to some of muono.}$$

- ... Wheel will travel in one revolution = $\frac{11}{7}$ m
- :. In 11 km, it will make revolutions

$$= 11 \text{ km} \div \frac{11}{7} \text{ m}$$

$$= 11000 \times \frac{7}{11} = 7000 \text{ revolutions}$$

- 18. The diameter of the wheels of a bus is 140 cm. How many revolutions per minute must a wheel make in order to move at a speed of 66 km per hour.
- Sol. Diameter of wheel = 140 cm.

$$\therefore \text{ Radius } (r) = \frac{140}{2} = 70 \text{ cm}$$

Circumference = $2\pi r^2 = 2 \times \frac{22}{7} \times 70$

$$= 440 \text{ cm} = \frac{440}{100} \text{ m}$$

Speed of bus = 66 km per hour.

: Number of revolutions in 1 hour

$$= \frac{66 \times 1000 \times 100}{440}$$
$$= 15000$$

$$\therefore \text{ Revolution in 1 minute} = \frac{15000}{60}$$
$$= 250 \text{ Ans.}$$

- 19. A bicycle wheel makes 5000 revolutions in moving 11 km. Find the diameter of the wheel.
- Sol. Number of revolutions = 5000 Distance = 11 km = 11000 m
 - .. Distance covered in one revolution

$$= \frac{11000}{5000} = \frac{11}{5} \text{ m}$$

:: Circumference of wheel of the cycle

$$=\frac{11}{5}$$
 m $=\frac{11}{5}$ × 100 = 220 cm

Let d be the diameter of the wheel $\pi d = 220$

$$\Rightarrow \frac{22}{7}d = 220$$

$$\Rightarrow d = \frac{220 \times 7}{22} = 70 \text{cm Ans.}$$

- 20. A square is inscribed in a circle whose radius is 4 cm. Find the area of the portion between the circle and the square.
- Sol. A square ABCD is inscribed in a circle with centre O.

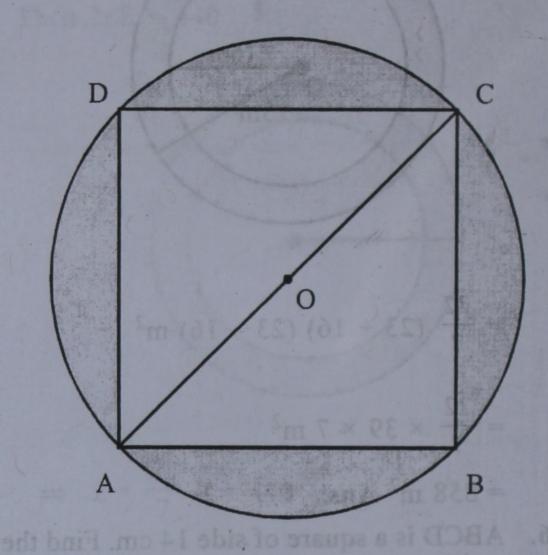
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Radius of circle = 4 cm

$$\therefore \text{ Diameter} = 4 \times 2 = 8 \text{ cm}$$

Let a be the side of the square

$$\therefore \quad \sqrt{2} \quad a = AC = 8$$



$$a = \frac{8}{\sqrt{2}} = \frac{8 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{8 \times \sqrt{2}}{2} = 4\sqrt{2}$$
 cm

Now area of circle = $\pi r^2 = \frac{22}{7} \times 4 \times 4 \text{ cm}^2$

$$=\frac{352}{7} \text{ cm}^2$$

and area of square = $(\text{side})^2 = (4\sqrt{2})^2 = 32 \text{ cm}^2$

$$\therefore \text{ Area of shaded portion} = \frac{352}{7} - 32$$

$$= \frac{352 - 224}{7} = \frac{128}{7} \text{ cm}^2$$

$$=18\frac{2}{7}=18.28 \text{ cm}^2 \text{ Ans}.$$