

## Constructions

In this chapter, we will revise some basic constructions that you learnt in the previous classes. You will also learn how to construct quadrilaterals, circumcircles and incircles. You will need only a ruler and a compass.

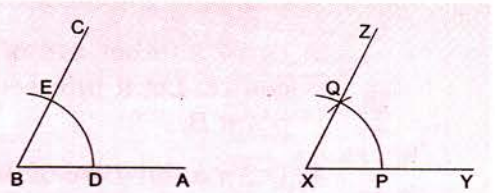
### Basic Constructions

#### To construct an angle equal to a given angle

**Construction 1** Construct an angle equal to  $\angle ABC$  at the point  $X$ .

**Steps of construction**

1. With  $B$  as the centre and a suitable radius, draw an arc to intersect  $BA$  at  $D$  and  $BC$  at  $E$ .
2. Draw a line  $XY$  through  $X$ .
3. With  $X$  as the centre and the same radius (as in Step 1), draw an arc which intersects  $XY$  at  $P$ .
4. With  $P$  as the centre and a radius equal to  $DE$ , draw an arc which intersects the arc drawn in Step 3 at  $Q$ .
5. Join  $X$  and  $Q$  and extend it to  $Z$ . Then,  $\angle YXZ$  is the required angle.

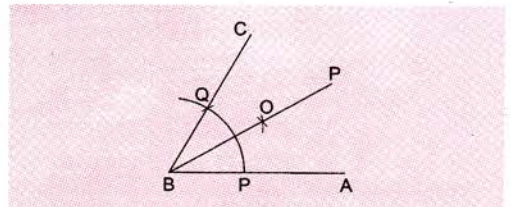


#### To bisect a given angle

**Construction 2** Bisect the given angle  $ABC$ .

**Steps of construction**

1. With  $B$  as the centre and a convenient radius, construct an arc which intersects  $BA$  at  $P$  and  $BC$  at  $Q$ .
2. With  $P$  as the centre and a suitable radius (more than half of  $PQ$ ), draw an arc.
3. With  $Q$  as the centre and the same radius, draw another arc to intersect the arc drawn in Step 2 at  $O$ .
4. Join  $B$  and  $O$  and extend it to  $P$ . Then, the ray  $BP$  bisects  $\angle ABC$ .

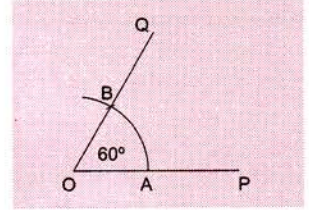


To construct angles of standard magnitudes

**Construction 3** Construct an angle of  $60^\circ$ .

**Steps of construction**

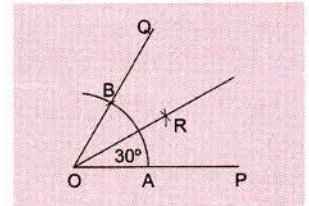
1. Draw a line  $OP$ .
2. With  $O$  as the centre and a suitable radius, draw an arc to intersect  $OP$  at  $A$ .
3. Draw another arc of the same radius with  $A$  as the centre. Let it intersect the arc drawn in Step 2 at the point  $B$ .
4. Draw a line joining  $O$  and  $B$  and extend it to  $Q$ .  
Then,  $\angle POQ$  is the required angle of  $60^\circ$ .



**Construction 4** Construct an angle of  $30^\circ$ .

**Steps of construction**

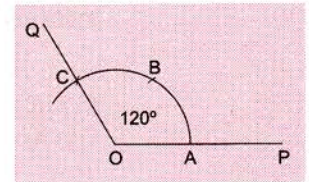
1. Draw  $\angle POQ$  of  $60^\circ$  as in the previous construction.
2. Bisect the  $\angle POQ$  as in Construction 2.
3. If  $OR$  is the bisector of  $\angle POQ$  then  
 $\angle POR = \angle QOR = 30^\circ$ .



**Construction 5** Construct an angle of  $120^\circ$ .

**Steps of construction**

1. Draw a line  $OP$ .
2. Draw an arc with  $O$  as the centre and a convenient radius to intersect  $OP$  at the point  $A$ .
3. Draw another arc of the same radius with  $A$  as the centre. Let it intersect the arc drawn in Step 2 at the point  $B$ .
4. Draw a third arc of the same radius with  $B$  as the centre so that it cuts the arc drawn in Step 2 at the point  $C$  (away from  $A$ ).
5. Draw a line joining  $O$  and  $C$  and extend it to  $Q$ .  
 $\angle QOP$  is an angle of measure  $120^\circ$ .

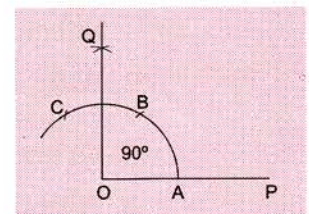


**Construction 6** Construct an angle of  $90^\circ$ .

**Steps of construction**

Follow the Steps 1 to 4 in the previous construction.

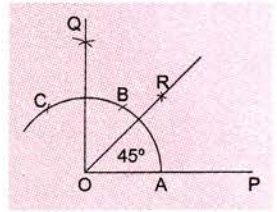
5. Draw an arc of a suitable radius (more than  $\frac{1}{2}BC$ ) with  $B$  as the centre.
6. Draw another arc of the same radius with  $C$  as the centre. Let this arc intersect the arc drawn in Step 5 at the point  $Q$ .
7. Draw a line through  $O$  and  $Q$ . Then  $\angle POQ = 90^\circ$ .



**Construction 7** Construct an angle of  $45^\circ$ .

**Steps of construction**

1. Follow the Steps in Construction 6 to draw  $\angle POQ = 90^\circ$ .
2. Bisect  $\angle POQ$  (see Construction 2). If  $OR$  is the bisector then  $\angle POR = \angle QOR = 45^\circ$ .

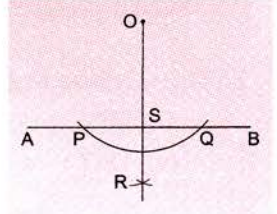


**To construct perpendicular lines**

**Construction 8** Construct a perpendicular to a line  $AB$  from an external point  $O$ .

**Steps of construction**

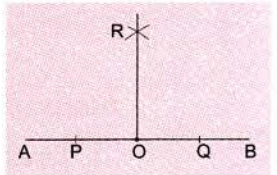
1. Draw a line  $AB$ .
2. Mark an external point  $O$ .
3. With  $O$  as the centre and a sufficiently large radius, draw an arc intersecting  $AB$  at the points  $P$  and  $Q$ .
4. With  $P$  as the centre and a radius more than  $\frac{1}{2}PQ$  ( $\neq OP$ ), draw another arc on any side of  $AB$ .
5. With  $Q$  as the centre and the same radius, draw a third arc, intersecting the arc drawn in Step 4 at the point  $R$ .
6. Draw a line joining  $O$  and  $R$ . Let it intersect  $AB$  at the point  $S$ . Then  $OS$  is the required perpendicular.



**Construction 9** Construct a line perpendicular to a line  $AB$  through a point  $O$  on the line.

**Steps of construction**

1. Draw a line  $AB$ .
2. Take a point  $O$  on  $AB$ .
3. Draw an arc with  $O$  as the centre and a convenient radius. Let it intersect the line  $AB$  at the points  $P$  and  $Q$ .
4. Draw an arc with  $P$  as the centre and a radius more than  $\frac{1}{2}PQ$ .
5. With  $Q$  as the centre and the same radius, construct another arc to intersect the arc drawn in Step 4 at the point  $R$ .
6. The line joining  $O$  and  $R$  is the perpendicular to the line  $AB$  at  $O$ .



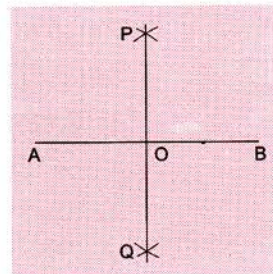
**To construct the perpendicular bisector of a line segment**

**Construction 10** Construct the perpendicular bisector of a line segment  $AB$ .

**Steps of construction**

1. Draw a line segment  $AB$ .
2. Draw two arcs with  $A$  as the centre and a radius more than  $\frac{1}{2}AB$ , one on each side of  $AB$ .

- With  $B$  as the centre and the same radius, construct two more arcs, one on each side of  $AB$  to intersect the arcs drawn in Step 2 at the points  $P$  and  $Q$  respectively.
- The line joining  $P$  and  $Q$  is the perpendicular bisector of  $AB$ . Let it intersect  $AB$  at  $O$ . Then,  $OA = OB = \frac{1}{2} AB$  and  $\angle AOP = \angle BOP = 90^\circ$ .



## EXERCISE

## 5A

- Draw a line segment  $BC = 6.3$  cm. Construct the following angles at the point  $B$ .
  - $30^\circ$
  - $60^\circ$
  - $90^\circ$
  - $45^\circ$
  - $120^\circ$
- Construct an angle of  $22\frac{1}{2}^\circ$ .
- Construct a line perpendicular to  $AB = 8$  cm through a point  $O$  on the line such that  $OA = 3.8$  cm.
- Draw a line segment  $PQ = 7.3$  cm. Take a point  $A$  above  $PQ$  such that  $AP = 4$  cm. Construct the perpendicular to  $PQ$  from  $A$ .
- Draw a line segment  $AB = 7.6$  cm and draw its perpendicular bisector  $PQ$ .

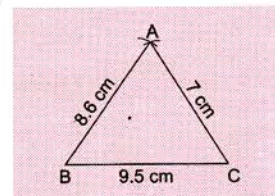
## Construction of Triangles

### To construct a triangle when three sides are known

**Construction 11** Construct a  $\triangle ABC$  such that  $AB = 8.6$  cm,  $BC = 9.5$  cm and  $AC = 7$  cm.

#### *Steps of construction*

- Draw a line segment  $BC = 9.5$  cm.
- Draw an arc of radius  $8.6$  cm with the centre at  $B$ .
- Draw an arc of radius  $7$  cm with the centre at  $C$ . Let this arc intersect the arc drawn in Step 2 at the point  $A$ .
- Join  $A$  to  $B$  and  $C$ . Then  $AB = 8.6$  cm,  $AC = 7$  cm and  $\triangle ABC$  is the required triangle.



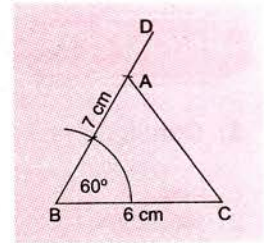
### To construct a triangle when two sides and the included angle are given

**Construction 12** Construct a triangle  $ABC$  in which  $BC = 6$  cm,  $AB = 7$  cm and  $\angle ABC = 60^\circ$ .

#### *Steps of construction*

- Draw a line segment  $BC$  of length  $6$  cm.

2. Draw an angle  $\angle CBD = 60^\circ$  at  $B$ . (See Construction 3.)
3. Draw an arc of radius 7 cm with the centre at  $B$ . Let this arc intersect  $BD$  at  $A$ . Then  $AB = 7$  cm.
4. Join  $A$  and  $C$ .  
 $\triangle ABC$  is the required triangle.

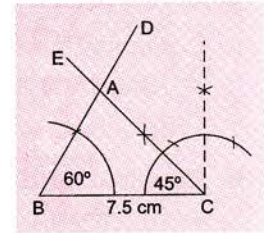


### To construct a triangle when one side and two angles are given

**Construction 13** Construct a triangle  $ABC$  in which  $BC = 7.5$  cm,  $\angle ABC = 60^\circ$  and  $\angle ACB = 45^\circ$ .

#### Steps of construction

1. Draw a line segment  $BC = 7.5$  cm.
2. Construct  $\angle CBD = 60^\circ$  at  $B$ . (See Construction 3.)
3. Construct  $\angle BCE = 45^\circ$  at  $C$ . (See Construction 7.)
4. Let  $CE$  and  $BD$  intersect at  $A$ .  
 $\triangle ABC$  is the required triangle.



**Note** If  $\angle BAC$  and  $\angle ABC$  are given, you will have to calculate  $\angle ACB$  by using  $\angle A + \angle B + \angle C = 180^\circ$ . Similarly, if  $\angle BAC$  and  $\angle ACB$  are given, you will have to calculate  $\angle ABC$ .

### To construct an equilateral triangle when its side is known

**Construction 14** Construct an equilateral triangle  $XYZ$  of side = 5 cm.

Proceed as in Construction 11. Here,  $XY = YZ = ZX = 5$  cm.

### To construct an isosceles triangle in which the base and the base angles are given

**Construction 15** Construct an isosceles triangle  $ABC$  in which  $BC = 6.5$  cm,  $\angle ABC = \angle ACB = 30^\circ$ .

Proceed as in Construction 13. Here,  $BC = 6.5$  cm,  $\angle ABC = 30^\circ$  and  $\angle ACB = 30^\circ$ .

### To construct an isosceles triangle in which the equal sides and the vertical angle are given

**Construction 16** Construct an isosceles  $\triangle ABC$  in which  $\angle BAC = 45^\circ$  and  $AB = AC = 6$  cm.

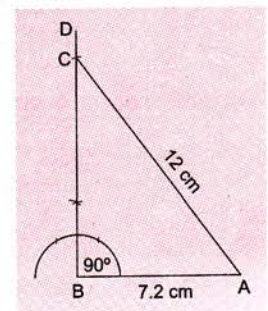
Proceed as in Construction 12. Here,  $AB = 6$  cm,  $AC = 6$  cm and the included  $\angle BAC = 45^\circ$ .

### To construct a right-angled triangle when a side and the hypotenuse are given

**Construction 17** Construct a right-angled triangle in which  $\angle ABC = 90^\circ$ ,  $AB = 7.2$  cm and  $AC = 12$  cm.

#### Steps of construction

1. Draw a line segment  $BA = 7.2$  cm.
2. Draw  $\angle ABD = 90^\circ$  at  $B$ .
3. With  $A$  as the centre, draw an arc of radius 12 cm. Let this arc intersect  $BD$  at  $C$ .
4. Join  $A$  and  $C$ .  $\triangle ABC$  is the required triangle.



**EXERCISE 5B**

- Construct a  $\triangle ABC$  in which
  - $AB = 6$  cm,  $BC = 5$  cm and  $AC = 4$  cm
  - the sides are 6.8 cm, 5 cm and 3.8 cm
- Construct a  $\triangle XYZ$  such that
  - $XY = 4$  cm,  $YZ = 6$  cm and  $\angle Y = 60^\circ$
  - $XY = 4.4$  cm,  $XZ = 3$  cm and  $\angle X = 120^\circ$
- Construct a  $\triangle PQR$  such that
  - $\angle P = 60^\circ$ ,  $\angle Q = 45^\circ$  and  $PQ = 7$  cm
  - $\angle Q = 60^\circ$ ,  $\angle R = 30^\circ$  and  $QR = 5.6$  cm
- Construct an equilateral triangle of side (i) 6 cm and (ii) 4.5 cm.
- Construct an isosceles triangle  $ABC$  in which
  - $AB = 4.8$  cm,  $\angle A = 30^\circ$ ,  $\angle B = 30^\circ$
  - $AB = 8.6$  cm,  $\angle A = 45^\circ$ ,  $\angle B = 45^\circ$
  - $\angle BAC = 60^\circ$ ,  $AB = AC = 6.5$  cm
  - $\angle ABC = 30^\circ$ ,  $AB = BC = 5$  cm
- Construct a right-angled triangle  $ABC$  in which
  - $\angle B = 90^\circ$ ,  $AC = 6$  cm,  $AB = 4$  cm
  - $\angle A = 90^\circ$ ,  $BC = 13$  cm,  $AC = 5$  cm
- Construct a right-angled triangle  $ABC$  in which  $\angle C = 90^\circ$ ,  $BC = 5$  cm,  $AC = 6$  cm.

**Construction of Quadrilaterals**

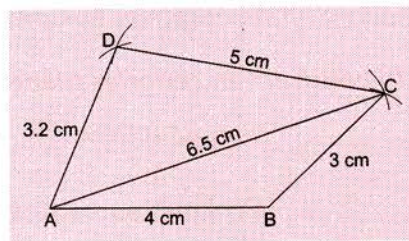
A quadrilateral has 10 elements (or parts)—four sides, four angles and two diagonals. Five elements are sufficient for constructing a quadrilateral.

**To construct a quadrilateral when four sides and one diagonal are given**

**Construction 18** Construct a quadrilateral  $ABCD$  in which  $AB = 4$  cm,  $BC = 3$  cm,  $CD = 5$  cm,  $DA = 3.2$  cm and  $AC = 6.5$  cm.

**Steps of construction**

- Draw a line segment  $AB = 4$  cm.
- With  $B$  as the centre, draw an arc of radius 3 cm.
- With  $A$  as the centre, draw an arc of radius 6.5 cm to intersect the arc drawn in Step 2 at  $C$ .
- With  $C$  as the centre, draw an arc of radius 5 cm.
- With  $A$  as the centre draw an arc of radius 3.2 cm to intersect the arc drawn in Step 4 at  $D$ .
- Join  $C$  and  $A$ ;  $C$  and  $B$ ;  $C$  and  $D$ ; and  $D$  and  $A$ .  
 $ABCD$  is the required quadrilateral.

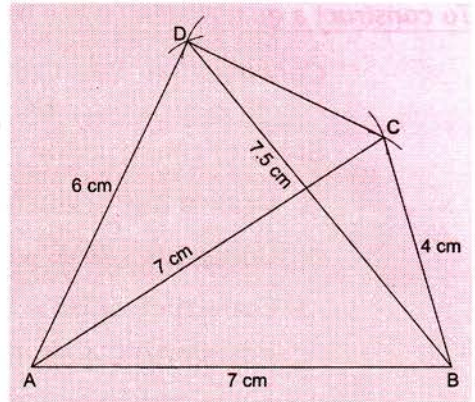
**To construct a quadrilateral when three sides and two diagonals are given**

**Construction 19** Construct a quadrilateral  $ABCD$  in which  $AB = 7$  cm,  $AD = 6$  cm,  $AC = 7$  cm,  $BD = 7.5$  cm and  $BC = 4$  cm.

**Steps of construction**

- Draw a line segment  $AB = 7$  cm.

- With  $A$  as the centre, draw an arc of radius 6 cm.
- With  $B$  as the centre, draw an arc of radius 7.5 cm to intersect the arc drawn in Step 2 at  $D$ .
- With  $A$  as the centre, draw an arc of radius 7 cm.
- With  $B$  as the centre, draw an arc of radius 4 cm to intersect the arc drawn in Step 4 at  $C$ .
- Join  $C$  and  $B$ ;  $C$  and  $A$ ;  $C$  and  $D$ ;  $D$  and  $A$  and  $D$  and  $B$ .  
 $ABCD$  is the required quadrilateral.

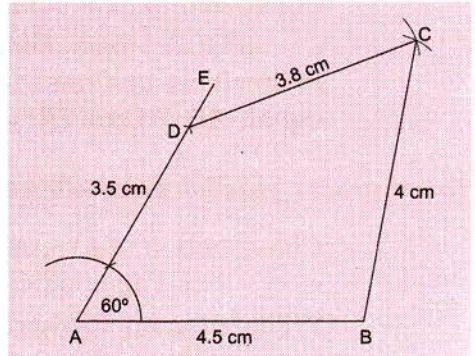


### To construct a quadrilateral when four sides and an angle are given

**Construction 20** Construct a quadrilateral  $ABCD$  in which  $AB = 4.5$  cm,  $BC = 4$  cm,  $CD = 3.8$  cm and  $AD = 3.5$  cm and  $\angle A = 60^\circ$ .

#### Steps of construction

- Draw a line segment  $AB = 4.5$  cm.
- Draw an angle  $\angle BAE = 60^\circ$  at  $A$ .
- Cut off  $AD = 3.5$  cm from  $AE$ .
- With  $D$  as the centre, draw an arc of radius 3.8 cm.
- With  $B$  as the centre, draw an arc of radius 4 cm to intersect the arc drawn in Step 4 at  $C$ .
- Join  $B$  and  $D$  to  $C$ .  
Then  $ABCD$  is the required quadrilateral.

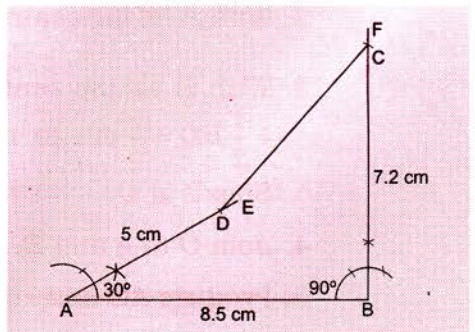


### To construct a quadrilateral when three sides and two included angles are given

**Construction 21** Construct a quadrilateral  $ABCD$  in which  $AB = 8.5$  cm,  $BC = 7.2$  cm,  $AD = 5$  cm,  $\angle B = 90^\circ$ ,  $\angle A = 30^\circ$ .

#### Steps of construction

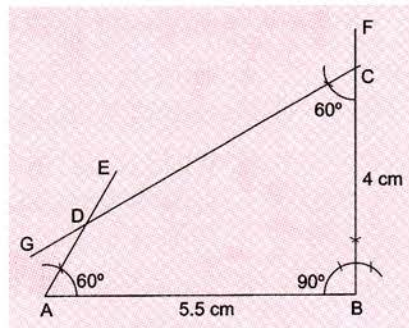
- Draw a line segment  $AB = 8.5$  cm.
- Construct  $\angle BAE = 30^\circ$  at  $A$ .
- Cut off  $AD = 5$  cm from  $AE$ .
- Construct  $\angle ABF = 90^\circ$  at  $B$ .
- Cut off  $BC = 7.2$  cm from  $BF$ .
- Join  $C$  and  $D$ .  
 $ABCD$  is the required quadrilateral.



**Construction 22** Construct a quadrilateral ABCD in which  $AB = 5.5$  cm,  $BC = 4$  cm,  $\angle A = 60^\circ$ ,  $\angle B = 90^\circ$  and  $\angle C = 60^\circ$ .

**Steps of construction**

1. Draw a line segment  $AB = 5.5$  cm.
  2. Construct  $\angle BAE = 60^\circ$  at A.
  3. Construct  $\angle ABF = 90^\circ$  at B.
  4. Cut off  $BC = 4$  cm from  $BF$ .
  5. Construct  $\angle BCG = 60^\circ$  at C.  $CG$  intersects  $AE$  at D.
- ABCD is the required quadrilateral.



**Note** If  $\angle D$  were given, we would have to find  $\angle C$  by using  $\angle C = 360^\circ - (\angle A + \angle B + \angle D)$ .

**Construction of parallelograms**

To construct a parallelogram when two adjacent sides and the included angle are given

**Construction 23** Construct a parallelogram ABCD in which  $AB = 6$  cm,  $AD = 8$  cm and  $\angle A = 60^\circ$ .

Proceed as in Construction 20. As the opposite sides of a parallelogram are equal,  $AB = 6$  cm,  $BC = 8$  cm,  $CD = 6$  cm,  $AD = 8$  cm and  $\angle A = 60^\circ$ .

To construct a parallelogram when two adjacent sides and one diagonal are given

**Construction 24** Construct a parallelogram ABCD in which  $AB = 5.2$  cm,  $BC = 4.8$  cm and  $AC = 7.4$  cm.

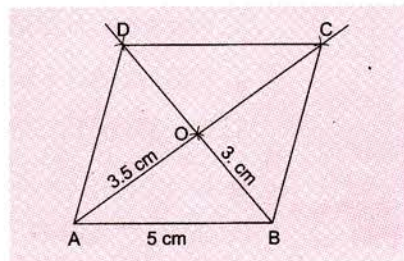
Proceed as in Construction 18. Since the opposite sides of a parallelogram are equal,  $AB = 5.2$  cm,  $BC = 4.8$  cm,  $CD = 5.2$  cm,  $AD = 4.8$  cm and  $AC = 7.4$  cm.

To construct a parallelogram when one side and both diagonals are given

**Construction 25** Construct a parallelogram ABCD in which  $AB = 5$  cm,  $AC = 7$  cm and  $BD = 6$  cm.

**Steps of construction**

1. Draw a line segment  $AB = 5$  cm.
2. With A as the centre, draw an arc of radius  $= \frac{1}{2} AC = 3.5$  cm.
3. With B as the centre, draw an arc of radius  $= \frac{1}{2} BD = 3$  cm to intersect the arc drawn in Step 2 at O.
4. Join O to A and B.
5. Produce AO and cut off  $OC = OA = 3.5$  cm.





6. Produce  $BO$  and cut off  $OD = OB = 3$  cm.
7. Join  $D$  and  $A$ ;  $D$  and  $C$ ; and  $C$  and  $B$ .  
 $ABCD$  is the required parallelogram.

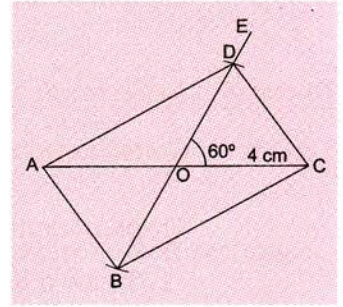
**To construct a parallelogram when the two diagonals and an angle between them are given**

**Construction 26** Construct a parallelogram  $ABCD$  in which  $AC = 4$  cm,  $BD = 5$  cm and an angle between them is  $60^\circ$ .

**Steps of construction**

1. Draw a line segment  $AC = 4$  cm.
2. Bisect  $AC$ . Let  $O$  be its mid-point.
3. Construct  $\angle COE = 60^\circ$  at  $O$ .
4. Cut off  $OD = \frac{1}{2}BD = 2.5$  cm from  $OE$ .
5. Produce  $DO$  and cut off  $OB = DO = 2.5$  cm.
6. Join  $D, A$ ;  $D, C$ ;  $A, B$  and  $B, C$ .

$ABCD$  is the required parallelogram.



**EXERCISE 5C**

1. Construct a quadrilateral  $ABCD$  in which
  - (i)  $AB = 4.5$  cm,  $BC = 4$  cm,  $CD = 6.5$  cm,  $DA = 3$  cm and  $BD = 6.5$  cm
  - (ii)  $AB = 4$  cm,  $BC = 3$  cm,  $AD = 2.5$  cm,  $AC = 4.5$  cm and  $BD = 10$  cm
  - (iii)  $AB = 6.4$  cm,  $BC = 5.8$  cm,  $AD = 3.6$  cm,  $CD = 3.6$  cm and  $\angle B = 45^\circ$
  - (iv)  $\angle B = 45^\circ$ ,  $\angle C = 90^\circ$ ,  $BC = 5$  cm,  $AB = 4$  cm and  $CD = 3$  cm
  - (v)  $AB = 4.5$  cm,  $BC = 3.8$  cm,  $\angle BCD = 90^\circ$ ,  $\angle BAD = 60^\circ$  and  $\angle ABC = 120^\circ$ .
2. Construct a parallelogram in which
  - (i)  $AB = 7.4$  cm,  $BC = 5.2$  cm and  $\angle ABC = 120^\circ$
  - (ii)  $AB = 3.6$  cm,  $BC = 4$  cm and  $AC = 6.5$  cm
  - (iii)  $AC = 8$  cm,  $BD = 14$  cm and  $CD = 8$  cm
  - (iv) diagonals are 6.5 cm and 4 cm long and angle between them is  $60^\circ$ .

## Construction of Rectangles

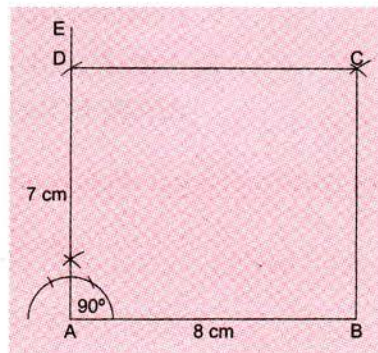
**To construct a rectangle when its length and breadth are given**

**Construction 27** Construct a rectangle  $ABCD$  with  $AB = 8$  cm and  $AD = 7$  cm.

**Steps of construction**

1. Draw a line segment  $AB = 8$  cm.
2. Construct  $\angle BAE = 90^\circ$  at  $A$ .

- Cut off  $AD = 7$  cm from  $AE$ .
- Draw an arc of radius 8 cm with  $D$  as the centre.
- Draw another arc of radius 7 cm with  $B$  as the centre to intersect the arc drawn in Step 4 at  $C$ .
- Join  $C$  to  $B$  and  $D$ .  
Then  $ABCD$  is the required rectangle.

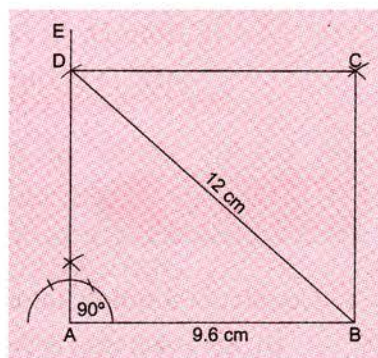


### To construct a rectangle when a side and a diagonal are given

**Construction 28** Construct a rectangle  $ABCD$  with  $AB = 9.6$  cm and  $BD = 12$  cm.

#### *Steps of construction*

- Draw a line segment  $AB = 9.6$  cm.
- Construct  $\angle BAE = 90^\circ$  at  $A$ .
- Draw an arc of radius 12 cm with  $B$  as the centre to intersect  $AE$  at  $D$ .
- Draw an arc of radius 9.6 cm with  $D$  as the centre.
- With  $B$  as the centre, draw an arc of radius equal to  $AD$  to intersect the arc drawn in Step 4 at  $C$ .
- Join  $C$  to  $B$  and  $D$ . Also, join  $B$  and  $D$ .  
 $ABCD$  is the required rectangle.

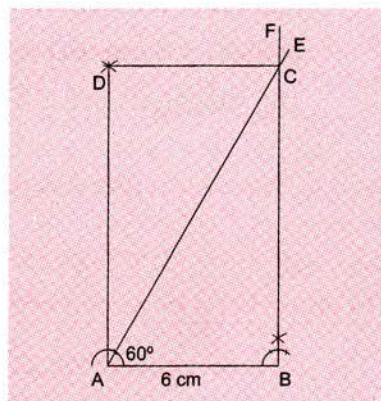


### To construct a rectangle when a side and the angle between the side and a diagonal are given

**Construction 29** Construct a rectangle  $ABCD$  with  $AB = 6$  cm and  $\angle BAC = 60^\circ$ .

#### *Steps of construction*

- Draw a line segment  $AB = 6$  cm.
- Construct  $\angle BAE = 60^\circ$  at  $A$ .
- Construct  $\angle ABF = 90^\circ$  at  $B$ , such that  $BF$  intersects  $AE$  at  $C$ .
- Draw an arc of radius 6 cm with  $C$  as the centre.
- Draw an arc of radius  $BC$  with  $A$  as the centre to intersect the arc drawn in Step 4 at  $D$ .
- Join  $C$  and  $A$  to  $D$ .



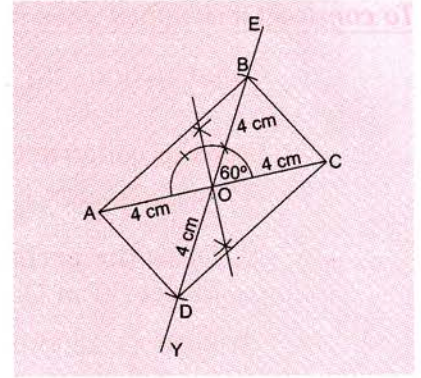
$ABCD$  is the required rectangle.

**To construct a rectangle when a diagonal and an angle between the two diagonals are given**

**Construction 30** Construct a rectangle  $ABCD$  with the diagonal  $AC = 8$  cm and an angle between the two diagonals  $= 60^\circ$ .

**Steps of construction**

1. Draw a line segment  $AC = 8$  cm.
2. Bisect  $AC$ . Let its mid-point be  $O$ .
3. Construct  $\angle COE = 60^\circ$  at  $O$ .
4. Cut off  $OB = \frac{1}{2} AC = 4$  cm from  $OE$ .
5. Produce  $BO$  to  $Y$ .
6. Cut off  $OD = \frac{1}{2} AC = 4$  cm from  $OY$ .
7. Join  $A$  to  $B$  and  $D$ , and  $C$  to  $B$  and  $D$ .



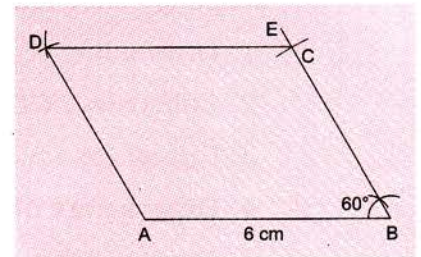
$ABCD$  is the required rectangle.

**Construction of rhombuses****To construct a rhombus when one side and one angle are given**

**Construction 31** Construct a rhombus  $ABCD$  with  $AB = 6$  cm and  $\angle ABC = 60^\circ$ .

**Steps of construction**

1. Draw a line segment  $AB = 6$  cm.
2. Construct  $\angle ABE = 60^\circ$  at  $B$ .
3. Cut off  $BC = 6$  cm from  $BE$ .
4. Draw an arc of radius 6 cm with  $C$  as the centre.
5. Draw another arc of radius 6 cm with  $A$  as the centre to intersect the arc drawn in Step 4 at  $D$ .
6. Join  $D$  to  $C$  and  $A$ .



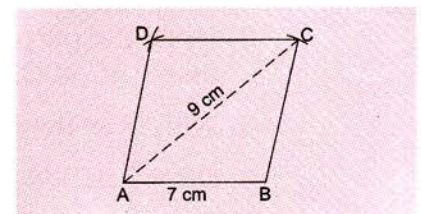
Thus,  $ABCD$  is the required rhombus.

**To construct a rhombus when a side and a diagonal are given**

**Construction 32** Construct a rhombus  $ABCD$  with  $AB = 7$  cm and diagonal  $AC = 9$  cm.

**Steps of construction**

1. Draw a line segment  $AB = 7$  cm.
2. With  $A$  as the centre, draw an arc of radius 9 cm.
3. With  $B$  as the centre, draw another arc of radius 7 cm to intersect the arc drawn in Step 2 at  $C$ .
4. With  $C$  as the centre, draw another arc of radius 7 cm.



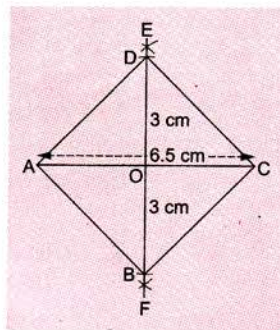
- Draw another arc of radius 7 cm with A as the centre to intersect the arc drawn in Step 4 at D.
- Join C to B, A and D, and D to A. ABCD is the required rhombus.

### To construct a rhombus when its diagonals are given

**Construction 33** Construct a rhombus ABCD, given  $AC = 6.5$  cm and  $BD = 6$  cm.

#### *Steps of construction*

- Draw a line segment  $AC = 6.5$  cm.
- Draw the perpendicular bisector  $EF$  of  $AC$ . Let  $EF$  bisect  $AC$  at  $O$ .
- With  $O$  as centre, cut off  $OD = \frac{1}{2}BD = 3$  cm and  $OB = \frac{1}{2}BD = 3$  cm from  $OE$  and  $OF$  respectively.
- Join  $D$  to  $A$  and  $C$ , and  $B$  to  $A$  and  $C$ .  
ABCD is the required rhombus.



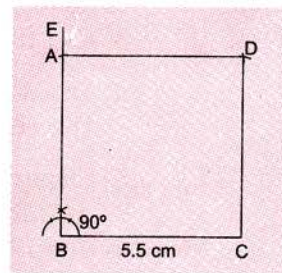
### **Construction of squares**

#### To construct a square when the side is given

**Construction 34** Construct a square ABCD, given  $BC = 5.5$  cm.

#### *Steps of construction*

- Draw a line segment  $BC = 5.5$  cm.
- Construct  $\angle CBE = 90^\circ$  at  $B$ .
- Cut off  $BA = 5.5$  cm from  $BE$ .
- Draw an arc of radius 5.5 cm with  $A$  as the centre.
- Draw another arc of radius 5.5 cm with  $C$  as the centre to intersect the arc drawn in Step 4 at  $D$ .
- Join  $A$  and  $C$  to  $D$ . ABCD is the required square.



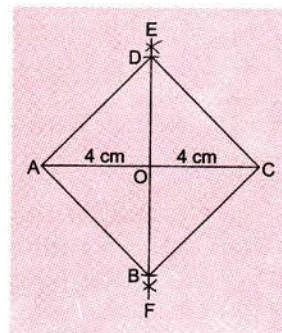
#### To construct a square when the diagonal is given

**Construction 35** Construct a square ABCD, given diagonal  $AC = 8$  cm.

#### *Steps of construction*

- Draw a line segment  $AC = 8$  cm.
- Draw the perpendicular bisector  $EF$  of  $AC$ . Let  $EF$  bisect  $AC$  at  $O$ .
- With  $O$  as the centre, cut off  $OD = \frac{1}{2}AC = 4$  cm and  $OB = \frac{1}{2}AC = 4$  cm from  $OE$  and  $OF$  respectively.
- Join  $B$  to  $A$  and  $C$  and  $D$  to  $A$  and  $C$ .

ABCD is the required square.



## EXERCISE

## 5D

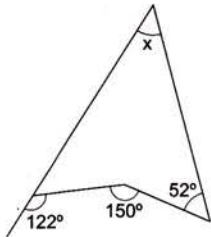
1. Construct a rectangle  $ABCD$  in which
  - (i)  $AB = 7$  cm and  $BC = 9$  cm
  - (ii)  $AB = 12$  cm and  $AC = 13$  cm
  - (iii)  $AB = 8$  cm and  $\angle BAC = 60^\circ$
  - (iv)  $BD = 7$  cm and an angle between the two diagonals =  $60^\circ$
2. Construct a rhombus  $ABCD$  in which
  - (i) each side =  $6$  cm and  $\angle B = 45^\circ$
  - (ii)  $AB = 4.7$  cm and  $AC = 6.2$  cm
  - (iii)  $AC = 6$  cm,  $BD = 4$  cm
3. Construct a square  $ABCD$  in which
  - (i) each side =  $5$  cm
  - (ii) diagonal  $AC = 9$  cm



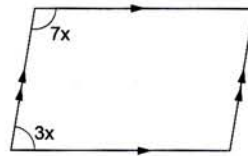
## Revision Exercise 2

- Find the sum of the interior angles of a 11-gon.
- The sum of the interior angles of a  $n$ -gon is  $8280^\circ$ . Find the value of  $n$ .
- Five angles of a polygon are  $162^\circ$  each and the remaining angles are  $150^\circ$  each. Find the number of sides of the polygon.
- Find the number of sides of a regular polygon if one of its interior angles equals  
(i)  $168^\circ 45'$  (ii)  $172^\circ 30'$ .
- Five angles of a nonagon are in the ratio  $9 : 10 : 11 : 12 : 13$  and rest of the angles equal  $120^\circ$  each. Find the largest angle.
- The sum of interior angles of a regular polygon is thrice the sum of its exterior angles. Find number of sides of the polygon.
- Find  $x$  in each of the following figures.

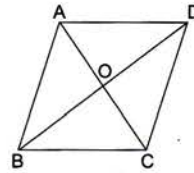
(i)



(ii)



- In the adjoining figure,  $ABCD$  is a rhombus. Prove that  $\triangle OAB \cong \triangle OAD$ .



- Construct a  $\triangle ABC$  in which

- $AB = 8$  cm,  $BC = 8.5$  cm and  $AC = 7$  cm
- $\angle A = 60^\circ$ ,  $AB = 3.8$  cm,  $AC = 5.5$  cm
- $\angle B = 30^\circ$ ,  $\angle C = 60^\circ$  and  $BC = 7$  cm
- $\angle A = 30^\circ$ ,  $\angle B = 45^\circ$  and  $AB = 6.3$  cm

- Construct a rectangle  $ABCD$  in which

- $AB = 8$  cm and  $BC = 8.7$  cm
- $AB = 6$  cm and  $BD = 6.5$  cm
- $BC = 6.8$  cm and  $\angle CBD = 45^\circ$
- $AC = 8$  cm and an angle between two diagonals  $= 30^\circ$

- Construct a rhombus  $PQRS$  in which

- each side  $= 7$  cm and  $\angle Q = 60^\circ$
- $QR = 7$  cm and  $QS = 8.5$  cm
- $PR = 7.3$  cm,  $QS = 6$  cm

- Construct a square  $ABCD$  in which

- each side  $= 6$  cm
- diagonal  $BD = 8$  cm

## ANSWERS

- |                                   |       |       |                   |                            |      |
|-----------------------------------|-------|-------|-------------------|----------------------------|------|
| 1. $1620^\circ$                   | 2. 48 | 3. 14 | 4. (i) 32 (ii) 48 | 5. $184\frac{4}{11}^\circ$ | 6. 8 |
| 7. (i) $40^\circ$ (ii) $18^\circ$ |       |       |                   |                            |      |

