

Similarity

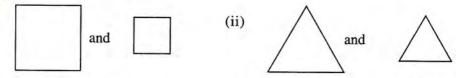
(With Applications to Maps and Models)

15.1 Introduction :

1. Similarity of Figures : Two figures are said to be similar, if they have the same shape but may differ in size.

Examples :





- (a) Same shape means : Angles of one figure are equal to corresponding angles of other figure each to each.
- (b) Same size means : Sides of one figure are equal to corresponding sides of the other figure each to each.
- 2. Congruency of Figures : Two figures are said to be *congruent*, if they have the same shape and the same size.

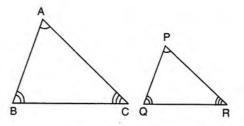
Congruent figures are always similar, whereas similar figures are not necessarily congruent.

15.2 Similar Triangles :

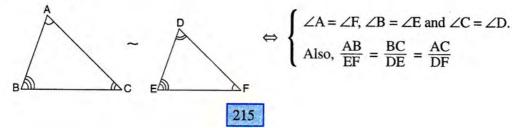
Two triangles are said to be *similar*, if their corresponding angles are *equal* and corresponding sides are *proportional* (*i.e.* the ratios between the lengths of corresponding sides are equal).

- e.g. Triangles ABC and PQR are similar, if :
- (a) their corresponding angles are equal
 - *i.e.* $\angle A = \angle P$, $\angle B = \angle Q$ and $\angle C = \angle R$
- (b) their corresponding sides are in proportion

i.e.
$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$
.



Symbolically, we write : \triangle ABC ~ \triangle PQR; where symbol ~ is read as, "is similar to". In the same way;

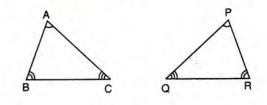


15.3 Corresponding sides and corresponding angles :

1. In similar triangles, the sides opposite to equal angles are said to be the corresponding sides.

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e.g. the adjoining figure shows, $\triangle ABC \sim \triangle PRQ$ in which $\angle A = \angle P$, $\angle B = \angle R$ and $\angle C = \angle Q$.

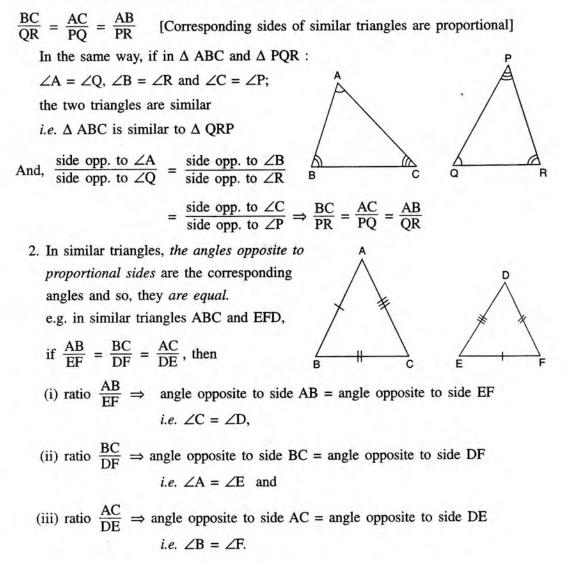


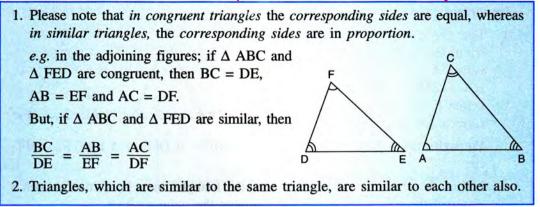
 $\therefore (i) \angle A = \angle P \qquad \Rightarrow \text{ Sides opposite to } \angle A \text{ and } \angle P \text{ are the corresponding sides.} \\ \Rightarrow \text{ Sides BC and QR are the corresponding sides.}$

(ii)
$$\angle B = \angle R$$
 \Rightarrow Sides opposite to $\angle B$ and $\angle R$ are the corresponding sides
 \Rightarrow Sides AC and PO are the corresponding sides.

Similarly, (iii) $\angle C = \angle Q \implies$ Sides AB and PR are the corresponding sides.

As, the triangles ABC and PRQ are similar; we have :





15.4 Condition of Similar Triangle : (SAS, AA or AAA and SSS)

1. If one angle of a triangle is equal to any angle of the other triangle and in both the triangles, the sides including the equal angles are in proportion; then the triangles are similar. (SAS postulate)

Example :

If in \triangle ABC and \triangle DEF,

$$\angle A = \angle D$$
 and $\frac{AB}{DE} = \frac{AC}{DF}$

then by SAS, Δ ABC ~ Δ DEF.

Similarly, if $\angle B = \angle E$ and $\frac{AB}{DE} = \frac{BC}{EF}$, then also $\triangle ABC \sim \triangle DEF$ and so on.

2. If two triangles have atleast two pairs of corresponding angles equal; the triangles are similar. (AA or AAA postulate)

Example :

If in \triangle ABC and \triangle DEF,

 $\angle A = \angle D$ and $\angle B = \angle E$, $\triangle ABC \sim \triangle DEF$.

Since, the sum of the angles of a triangle is 180°, therefore if two angles of one triangle are equal to two angles of another triangle each to each, their third angles are also equal.

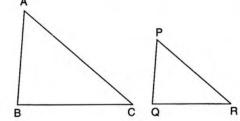
- 3. If two triangles have their three pairs of corresponding sides proportional, then the triangles are similar. (SSS postulate)

Example :

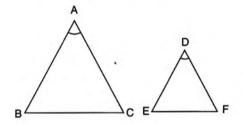
If in \triangle ABC and \triangle PQR,

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$

 Δ ABC ~ Δ PQR.



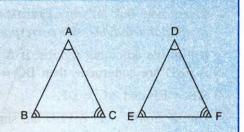
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Important :

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The given figure shows two similar triangles ABC and DEF such that vertex A corresponds to vertex D (as, ∠A = ∠D); vertex B corresponds to vertex E (as, ∠B = ∠E) and, vertex C corresponds to vertex F (as, ∠C = ∠F).



AC E

AC

EÁ

We write : \triangle ABC ~ \triangle DEF and not \triangle ABC ~ \triangle DFE or \triangle BAC ~ \triangle DEF, etc.

In fact, the order of vertices of two similar triangles must be written in such a way that the corresponding vertices occupy the same position.

BA

BA

Thus, triangle ABC is similar to triangle DEF

$$\Rightarrow \Delta \overrightarrow{ABC} \sim \Delta \overrightarrow{DEF} [A \leftrightarrow D, B \leftrightarrow E \text{ and } C \leftrightarrow F]$$

2. The adjoining figure shows two similar triangles such that, the corresponding vertices are:

 $A \leftrightarrow E; B \leftrightarrow D \text{ and } C \leftrightarrow F.$

$$\therefore \Delta ABC \sim \Delta EDF$$

3. In the adjoining figure, the corresponding vertices are : A and F, B and D and C and E.

 $\therefore \Delta ABC \sim \Delta FDE$

A perpendicular drawn from the vertex of the right angle of a right-angled triangle divides the triangle into two triangles similar to each other and also to the original triangle. Prove it.

Solution :

1

Let ABC be a right angled triangle, right angled at vertex A and AD is perpendicular drawn to the hypotenuse BC.

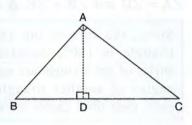
To Prove : \triangle DBA ~ \triangle DAC ~ \triangle ABC

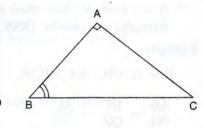
Proof :

Statement :

- 1. In \triangle DBA and \triangle ABC :
 - (i) $\angle ABD = \angle ABC$ [Common]
 - (ii) $\angle ADB = \angle BAC$ [Each 90°]
 - $\therefore \Delta DBA \sim \Delta ABC$ [AA or AAA postulate]

Reason



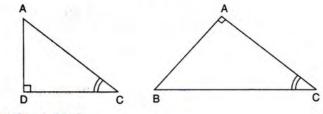


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2. In \triangle DAC and \triangle ABC :

- (i) $\angle ACD = \angle ACB$ [Common]
- (ii) $\angle ADC = \angle BAC$ [Each 90°]

 $\therefore \Delta DAC \sim \Delta ABC$ [AA or AAA postulate]

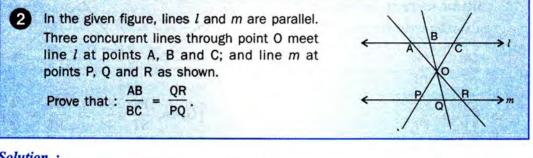


3. ∴ Δ DBA ~ Δ DAC ~ Δ ABC

[From 1 and 2]

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Hence Proved.



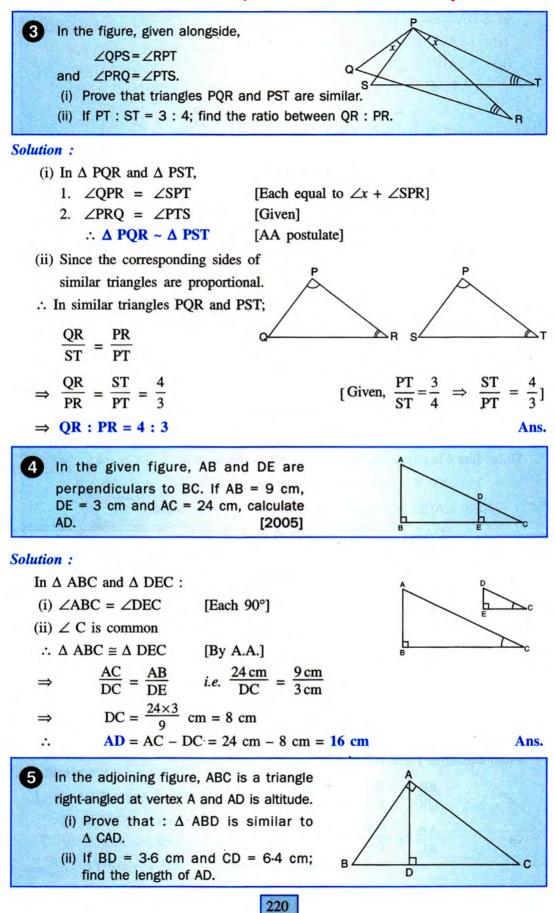
Solution :

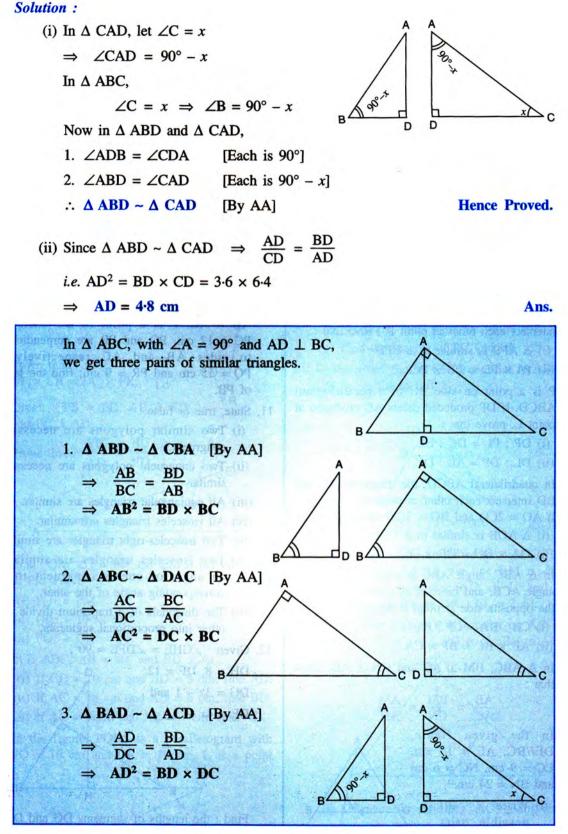
Since, line	e l is paral	lel to line m	and AR is transversal
÷.	∠OAB =	∠ORQ	[Alternate angles]
Also,	∠AOB =	∠QOR	[Vertically opposite angles]
÷	ΔΟΑΒ ~	ΔORQ	[By A.A. postulate] $(P_{M}) \xrightarrow{R} m$
⇒	$\frac{AB}{QR} =$	• <u>OB</u> I	[Corresponding sides of similar triangles are in proportion]
Similarly,	∠OCB =	- ∠OPQ	[Alternate angles]
and,	∠BOC =	- ∠POQ	[Vertically opposite angles]
÷	ΔBOC ~	ΔQOP	[By A.A. postulate]
⇒	$\frac{BC}{PQ} =$	= <u>OB</u> II	[Corresponding sides of similar Δs]
From equa	ations I an	d II, we get :	

 $\frac{AB}{QR} = \frac{BC}{PQ}$ $\frac{AB}{BC} = \frac{QR}{PQ}$

Hence proved.

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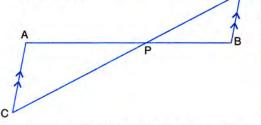


EXERCISE 15(A)

- 1. In the figure, given below, straight lines AB and CD intersect at P; and AC // BD. Prove that :
 - (i) \triangle APC and \triangle BPD are similar.

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(ii) If BD = 2.4 cm, AC = 3.6 cm, PD = 4.0 cm and PB = 3.2 cm; find the lengths of PA and PC.



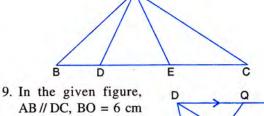
- 2. In a trapezium ABCD, side AB is parallel to side DC; and the diagonals AC and BD intersect each other at point P. Prove that :
 - (i) \triangle APB is similar to \triangle CPD.
 - (ii) $PA \times PD = PB \times PC$.
- 3. P is a point on side BC of a parallelogram ABCD. If DP produced meets AB produced at point L, prove that :
 - (i) DP : PL = DC : BL.
 - (ii) DL : DP = AL : DC.
- 4. In quadrilateral ABCD, the diagonals AC and BD intersect each other at point O.
 If AO = 2CO and BO = 2DO; show that :
 (i) Δ AOB is similar to Δ COD.
 - (ii) $OA \times OD = OB \times OC$.
- 5. In \triangle ABC, angle ABC is equal to twice the angle ACB, and bisector of angle ABC meets the opposite side at point P. Show that :
 - (i) CB : BA = CP : PA
 - (ii) $AB \times BC = BP \times CA$
- 6. In \triangle ABC; BM \perp AC and CN \perp AB; show that :

D

$$\frac{AB}{AC} = \frac{BM}{CN} = \frac{AM}{AN}$$

- 7. In the given figure, DE//BC, AE = 15 cm, EC = 9 cm, NC = 6 cm and BN = 24 cm.
 - (i) Write all possible pairs of similar triangles.
 - (ii) Find lengths of ME and DM.

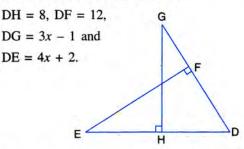
8. In the given figure, AD = AE and AD² = BD × EC.
Prove that : triangles ABD and CAE are similar.



C

AB // DC, BO = 6 cm and DQ = 8 cm; find: BP \times DO.

- 10. Angle BAC of triangle ABC is obtuse and AB = AC. P is a point in BC such that PC = 12 cm. PQ and PR are perpendiculars to sides AB and AC respectively. If PQ = 15 cm and PR = 9 cm; find the length of PB.
- 11. State, true or false :
 - (i) Two similar polygons are necessarily congruent.
 - (ii) Two congruent polygons are necessarily similar.
 - (iii) All equiangular triangles are similar.
 - (iv) All isosceles triangles are similar.
 - (v) Two isosceles-right triangles are similar.
 - (vi) Two isosceles triangles are similar, if an angle of one is congruent to the corresponding angle of the other.
 - (vii) The diagonals of a trapezium divide each other into proportional segments.
- 12. Given : $\angle GHE = \angle DFE = 90^\circ$,



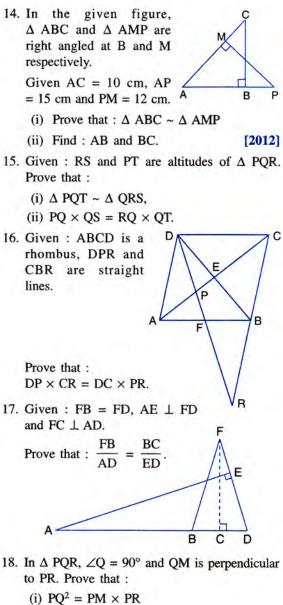
Find : the lengths of segments DG and DE.

13. D is a point on the side BC of triangle ABC such that angle ADC is equal to angle BAC. Prove that : $CA^2 = CB \times CD$.

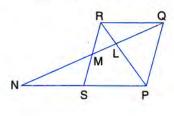
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M

N



- (i) $R^2 = R \times MR$
- (iii) $PQ^2 + QR^2 = PR^2$
- $(m) PQ^{-} + QR^{-} = PR^{-}$
- 19. In \triangle ABC, \angle B = 90° and BD \perp AC.
 - (i) If CD = 10 cm and BD = 8 cm; find AD.
 - (ii) If AC = 18 cm and AD = 6 cm; find BD.
 - (iii) If AC = 9 cm and AB = 7 cm; find AD.
- 20. In the figure, PQRS is a parallelogram with PQ = 16 cm and QR = 10 cm. L is a point



on PR such that RL : LP = 2 : 3. QL produced meets RS at M and PS produced at N.

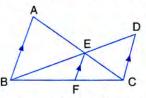
Find the lengths of PN and RM.

21. In quadrilateral ABCD, diagonals AC and BD intersect at point E such that

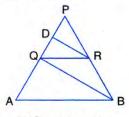
AE : EC = BE : ED.

Show that : ABCD is a trapezium.

- 22. In triangle ABC, AD is perpendicular to side BC and $AD^2 = BD \times DC$. Show that angle BAC = 90°.
- 23. In the given figure, AB // EF // DC; AB = 67.5 cm, DC = 40.5 cm and AE = 52.5 cm.

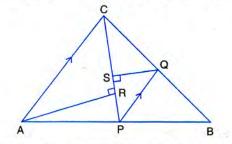


- (i) Name the three pairs of similar triangles.
- (ii) Find the lengths of EC and EF.
- 24. In the given figure, QR is parallel to AB and DR is parallel to QB.



Prove that : $PQ^2 = PD \times PA$.

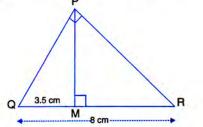
- 25. Through the mid-point M of the side CD of a parallelogram ABCD, the line BM is drawn intersecting diagonal AC in L and AD produced in E. Prove that : EL = 2 BL.
- 26. In the given figure, P is a point on AB such that AP : PB = 4 : 3. PQ is parallel to AC.



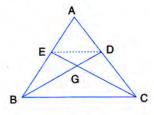
- (i) Calculate the ratio PQ : AC, giving reason for your answer.
- (ii) In triangle ARC, ∠ARC = 90° and in triangle PQS, ∠PSQ = 90°. Given QS = 6 cm, calculate the length of AR.

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27. In the right-angled triangle QPR, PM is an altitude.



Given that QR = 8 cm and MQ = 3.5 cm, calculate the value of PR. [2000] 28. In the figure, given below, the medians BD and CE of a triangle ABC meet at G. Prove that :



(i) \triangle EGD ~ \triangle CGB and (ii) BG = 2 GD from (i) above.

15.5 Basic Proportionality Theorem With Applications :

Theorem 1

A line drawn parallel to one side of a triangle divides the other two sides proportionally.

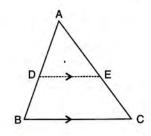
Given : In \triangle ABC; line DE is drawn parallel to side BC which meets AB at D and AC at E.

To Prove :
$$\frac{AD}{DB} = \frac{AE}{EC}$$

Proof :

7

Statement :



Reason :

In \triangle ABC and \triangle ADE,

1.		$\angle ABC = \angle ADE$
2.		∠ACB =∠AED
3.		∠BAC =∠DAE
		\triangle ABC ~ \triangle ADE
	÷	$\frac{AB}{AD} = \frac{AC}{AE}$
	⇒	$\frac{AD + DB}{AD} = \frac{AE + EC}{AE}$
	⇒	$1 + \frac{DB}{AD} = 1 + \frac{EC}{AE}$
	⇒	$\frac{DB}{AD} = \frac{EC}{AE}$
	⇒	$\frac{AD}{DB} = \frac{AE}{EC}$

[Corresponding angles] [Corresponding angles] [Common] [AAA postulate]

[Corresponding sides of similar triangles are proportional]

 $\left[\frac{AD}{AD} = 1 \text{ and } \frac{AE}{AE} = 1\right]$

[Cancelling 1 from both the sides]

[Taking the reciprocal]

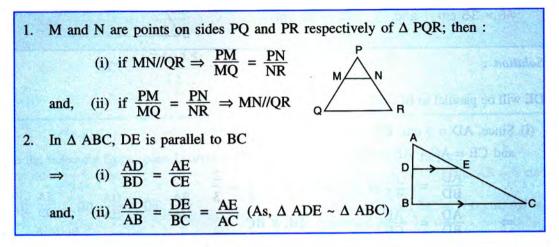
Hence Proved.

224

Conversely: If a line divides any two sides of a triangle proportionally, the line is parallel to the third side.

Note : In \triangle ABC, D is a point in AB and E is a point AC

such that $\frac{AD}{BD} = \frac{AE}{CE}$, then DE//BC.



6 In the adjoining figure; DE // BC and D divides AB in the ratio 2 : 3. Find : (i) $\frac{AE}{EC}$ (ii) $\frac{AE}{AC}$ (iii) DE, if BC = 7.5 cm.

Solution :

 (i) Since, a line drawn parallel to one side of a triangle, divides the other two sides proportionally;

 $\therefore \qquad \frac{AD}{DB} = \frac{AE}{EC} \qquad \dots \qquad I$

Also, given that D divides AB in the ratio 2 : 3 *i.e.* $\frac{AD}{DB} = \frac{2}{3}$ II

From I and II, we get : $\frac{AE}{EC} = \frac{2}{3}$

(iii)

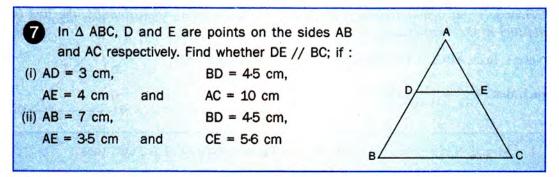
$$\frac{AE}{AC} = \frac{AE}{AE+EC} = \frac{2}{2+3} = \frac{2}{5}$$

$$\frac{AD}{AB} = \frac{DE}{BC} = \frac{AE}{AC}$$
 [As, \triangle ADE ~ \triangle ABC]

$$\frac{DE}{7\cdot5} = \frac{2}{5} \qquad [From (ii), \frac{AE}{AC} = \frac{2}{5}]$$
$$DE = \frac{2}{5} \times 7\cdot5 \text{ cm} = 3 \text{ cm}$$

Ans.

Ans.



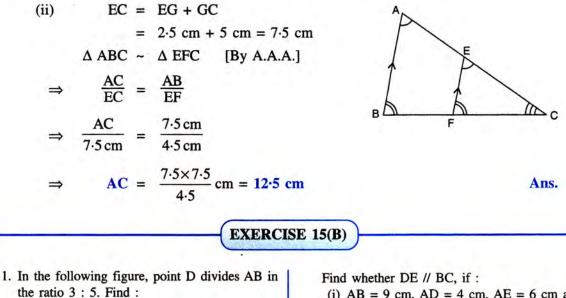
Solution :

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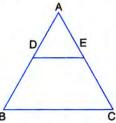
DE will be parallel to BC, only when $\frac{AD}{BD} = \frac{AE}{CE}$ (i) Since, AD = 3 cm, BD = 4.5 cm; AE = 4 cm and CE = AC - AE = 10 cm - 4 cm = 6 cm. $\frac{AD}{BD} = \frac{3}{4\cdot 5} = \frac{2}{3}$ and, $\frac{AE}{CE} = \frac{4}{6} = \frac{2}{3}$... $\frac{AD}{BD} = \frac{AE}{CE} \qquad \therefore \quad DE // BC$ => $\frac{AD}{BD} = \frac{AB - BD}{BD} = \frac{7 - 4.5}{4.5} = \frac{2.5}{4.5} = \frac{5}{9}$ (ii) Ans. $\frac{AE}{CE} = \frac{3.5}{5.6} = \frac{5}{8}$ and, $\frac{AD}{BD} \neq \frac{AE}{CE} \Rightarrow DE$ is not parallel to BC. Since, Ans. 8 In the given figure; AB//EF//CD. Given that ^A AB = 7.5 cm, EG = 2.5 cm, GC = 5 cm and DC = 9 cm. Calculate : (i) EF (ii) AC. в

Solution :

(i) In \triangle EGF and \triangle CGD, \angle EGF = \angle CGD [Vertically opposite angles] and, \angle EFG = \angle D [Alternate angles] $\therefore \triangle$ EGF ~ \triangle CGD [By A.A. postulate] $\Rightarrow \frac{EF}{DC} = \frac{EG}{GC}$ [Corresponding parts of similar triangles are proportional] $\Rightarrow \frac{EF}{9 \text{ cm}} = \frac{2.5 \text{ cm}}{5 \text{ cm}}$ $\Rightarrow EF = \frac{2.5}{5} \times 9 \text{ cm} = 4.5 \text{ cm}$ Ans. 226

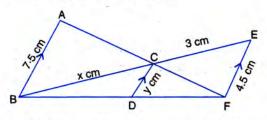


- (i) AB = 9 cm, AD = 4 cm, AE = 6 cm and EC = 7.5 cm.
- (ii) AB = 6.3 cm, EC = 11.0 cm, AD = 0.8 cm and AE = 1.6 cm.
- 5. In the given figure, $\triangle ABC \sim \triangle ADE$. If AE : EC = 4 : 7 and DE = 6.6 cm, find BC. If 'x' be the length of the perpendicular from

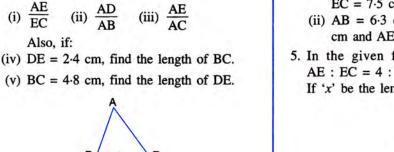


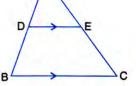
A to DE, find the length of perpendicular from A to BC in terms of 'x'.

- 6. A line segment DE is drawn parallel to base BC of \triangle ABC which cuts AB at point D and AC at point E. If AB = 5 BD and EC = 3.2 cm, find the length of AE.
- 7. In the figure, given below, AB, CD and EF are parallel lines. Given AB = 7.5 cm, DC = y cm, EF = 4.5 cm, BC = x cm and CE = 3 cm, calculate the values of x and y.

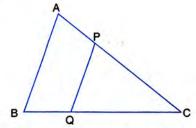


8. In the figure, given below, PQR is a rightangle triangle right angled at Q. XY is parallel

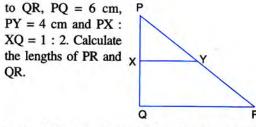




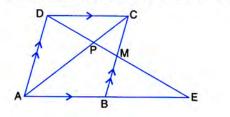
- 2. In the given figure, PQ // AB; CQ = 4.8 cm QB = 3.6 cm and AB = 6.3 cm. Find :
 - (i) $\frac{CP}{PA}$ (ii) PQ
 - (iii) If AP = x, then the value of AC in terms of x.



- 3. A line PQ is drawn parallel to the side BC of \triangle ABC which cuts side AB at P and side AC at Q. If AB = 9.0 cm, CA = 6.0 cm and AQ = 4.2 cm, find the length of AP.
- 4. In \triangle ABC, D and E are the points on sides AB and AC respectively.

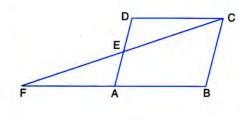


9. In the following figure, M is mid-point of BC of a parallelogram ABCD. DM intersects the



diagonal AC at P and AB produced at E. Prove that : PE = 2 PD

10. The given figure shows a parallelogram ABCD. E is a point in AD and CE produced meets BA produced at point F. If AE = 4 cm, AF = 8 cm and AB = 12 cm, find the perimeter of the parallelogram ABCD.



A C

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15.6 Relation between the areas of two triangles :

Theorem 2

The areas of two similar triangles are proportional to the squares on their corresponding sides.

B

Given : \triangle ABC ~ \triangle DEF

such that $\angle BAC = \angle EDF$,

 $\angle B = \angle E$ and $\angle C = \angle F$.

To Prove :

$$\frac{\text{Area of } \Delta \text{ ABC}}{\text{Area of } \Delta \text{ DEF}} = \frac{\text{AB}^2}{\text{DE}^2} = \frac{\text{BC}^2}{\text{EF}^2} = \frac{\text{AC}^2}{\text{DF}^2}$$

Construction :

Draw AM \perp BC and DN \perp EF.

Proof :

1.

Statement

Reason

Area of
$$\triangle ABC = \frac{1}{2}BC \times AM$$

Area of $\triangle DEF = \frac{1}{2}EF \times DN$
 $\Rightarrow \frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle DEF} = \frac{\frac{1}{2}BC \times AM}{\frac{1}{2}EF \times DN}$
 $= \frac{BC}{EF} \times \frac{AM}{DN}$
Area of $\triangle DEF$

228

2. In \triangle ABM and \triangle DEN : (i) $\angle B = \angle E$ [Given] (ii) $\angle AMB = \angle DNE$ [Each angle being 90°] $\therefore \triangle$ ABM ~ \triangle DEN [By AA postulate] $\Rightarrow \frac{AM}{DN} = \frac{AB}{DE}$ II [Corresponding sides of similar triangles are in proportion] 3. Since, \triangle ABC ~ \triangle DEF [Given]

[Corresponding sides of similar triangles are in proportion]

.....IV

Hence Proved.

$$\therefore \frac{AM}{DN} = \frac{BC}{EF}$$
[From II and III]
Substituting $\frac{AM}{EF} = \frac{BC}{EF}$ in equation I, we get :

$$\frac{\text{Area of } \Delta \text{ ABC}}{\text{Area of } \Delta \text{ DEF}} = \frac{\text{BC}}{\text{EF}} \times \frac{\text{BC}}{\text{EF}} = \frac{\text{BC}^2}{\text{EF}^2}$$

EF

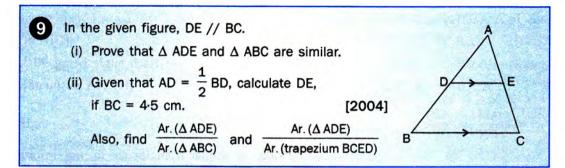
Now combining eq. III and eq. IV, we get :

DN

$$\frac{\text{Area of } \Delta \text{ ABC}}{\text{Area of } \Delta \text{ DEF}} = \frac{\text{AB}^2}{\text{DE}^2} = \frac{\text{BC}^2}{\text{EF}^2} = \frac{\text{AC}^2}{\text{DF}^2}$$

Remember :

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Solution :

...

10

1

(i) DE // BC $\Rightarrow \angle ADE = \angle ABC$ and, $\angle AED = \angle ACB$

 \triangle ADE ~ \triangle ABC

[Corresponding angles] [Corresponding angles] [By A.A.]

Hence Proved.

(ii) Since the corresponding sides of the similar triangles are in proportion : $\therefore \quad \frac{DE}{BC} = \frac{AD}{AB}$ i.e. $\frac{DE}{4.5 \text{ cm}} = \frac{1}{3}$ $\Rightarrow \quad DE = \frac{1}{3} \times 4.5 \text{ cm} = 1.5 \text{ cm}$ Ans. Given, $AD = \frac{1}{2}$ $Since, \quad \frac{AD}{BD} = \frac{1}{2}$ $\Rightarrow \quad \frac{AD}{AD + BD} = \frac{1}{1+2}$ $\Rightarrow \quad \frac{AD}{AB} = \frac{1}{3}$

We know the ratio between the areas of two similar triangles

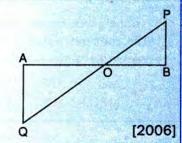
= ratio between the squares of its corresponding sides.

$$\frac{\text{Ar.}(\Delta \text{ ADE})}{\text{Ar.}(\Delta \text{ ABC})} = \frac{\text{DE}^2}{\text{BC}^2} = \frac{(1\cdot5)^2}{(4\cdot5)^2} = \frac{1}{9}$$
Ans.
$$\frac{\text{Ar.}(\Delta \text{ ADE})}{\frac{1}{1+(\Delta + \text{DE})} = \frac{1}{2}}$$

$$\Rightarrow \quad \frac{AI.(\Delta ADE)}{Ar.(\Delta ABC) - Ar.(\Delta ADE)} = \frac{1}{9-1}$$

$$\Rightarrow \qquad \frac{\text{Ar.}(\Delta \text{ ADE})}{\text{Ar.}(\text{trapezium BCED})} = \frac{1}{8}$$

In the figure, given alongside, PB and QA are perpendiculars to the line segment AB. If PO = 6 cm, QO = 9 cm and area of Δ POB = 120 cm², find the area of Δ QOA.



Ans.

230

Solution :

ż

In \triangle POB and \triangle QOA :

1. $\angle PBO = \angle QAO$ ∠POB = ∠QOA 2.

 Δ POB ~ Δ QOA \Rightarrow

$$\Rightarrow \qquad \frac{\text{Ar.}(\Delta \text{POB})}{\text{Ar.}(\Delta \text{QOA})} = \frac{\text{PO}^2}{\text{QO}^2}$$

[By A.A.]

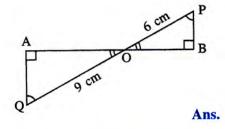
[Vertically opposite angles]

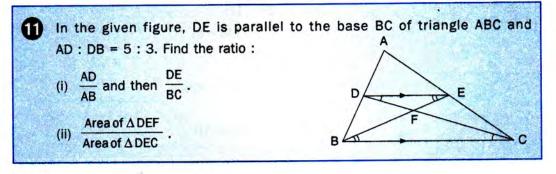
[Each 90°]

Ans.

[Ratio between the areas of two similar triangles is equal to the ratio between the squares of the corresponding sides]

$$\Rightarrow \frac{120}{\text{Ar.}(\Delta \text{QOA})} = \frac{6^2}{9^2}$$
$$\Rightarrow \text{Ar.} (\Delta \text{QOA}) = \frac{120 \times 81}{36} \text{ cm}^2$$
$$= 270 \text{ cm}^2$$





Solution :

(i)
$$\frac{AD}{DB} = \frac{5}{3} \implies \frac{AD}{AD + DB} = \frac{5}{5+3}$$

 $\Rightarrow \frac{AD}{AB} = \frac{5}{8}$ Ans.
Since, $\triangle ADE \sim \triangle ABC$ [By AA postulate]

Since, \triangle ADE ~ \triangle ABC

$$\Rightarrow \qquad \frac{DE}{BC} = \frac{AD}{AB} = \frac{5}{8}$$

(ii) Since, \triangle DEF and \triangle DEC have common vertex at E and their bases DF and DC are along the same straight line

$$\therefore \frac{\text{Area of } \Delta \text{ DEF}}{\text{Area of } \Delta \text{ DEC}} = \frac{\text{DF}}{\text{DC}} \qquad \dots (I)$$

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Now, show that \triangle DFE ~ \triangle CFB

$$\Rightarrow \frac{DF}{FC} = \frac{DE}{BC} = \frac{5}{8}$$

$$\Rightarrow \frac{DF}{DF + FC} = \frac{5}{5 + 8} \Rightarrow \frac{DF}{DC} = \frac{5}{13} \qquad \dots (II)$$
From I and II, we get : $\frac{\text{Area of } \Delta \text{ DEF}}{\text{Area of } \Delta \text{ DEC}} = \frac{5}{13}$
Ans.

12 In $\Delta \text{ ABC}$, $\angle B = 90^\circ$, $AB = 12$ cm and $AC = 15$ cm.
D and E are points on AB and AC respectively such that $\angle AED = 90^\circ$ and $DE = 3$ cm. Calculate the area of $\Delta \text{ ABC}$ and then the area of $\Delta \text{ ADE}$.

Solution :

 \Rightarrow

7

In right-angled triangle ABC,

 $AB^2 + BC^2 = AC^2$ [Pythagoras theorem] $BC^2 = 15^2 - 12^2$ \Rightarrow = 225 - 144 = 81 $BC = 9 \, cm$ Area of \triangle ABC = $\frac{1}{2}$ × base × height ... $=\frac{1}{2} \times BC \times AB$ $=\frac{1}{2} \times 9 \times 12 \text{ cm}^2 = 54 \text{ cm}^2$ Ans. In \triangle ADE and \triangle ABC, $\angle ABC = \angle AED = 90^{\circ}$ and $\angle A$ is common to both. : By A.A. axiom, \triangle ADE ~ \triangle ABC $\frac{\text{Ar. of } \Delta \text{ ADE}}{\text{Ar. of } \Delta \text{ ABC}} = \frac{\text{DE}^2}{\text{BC}^2}$ B \Rightarrow $\frac{\text{Ar. of } \Delta \text{ ADE}}{54 \text{ cm}^2} = \frac{3^2}{9^2}$ =

Ar. of
$$\triangle$$
 ADE = $\frac{9}{81} \times 54 \text{ cm}^2$
= 6 cm²

Ans.

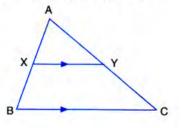
2C

EXERCISE 15(C)

- 1. (i) The ratio between the corresponding sides of two similar triangles is 2 is to 5. Find the ratio between the areas of these triangles.
 - (ii) Areas of two similar triangles are 98 sq. cm and 128 sq. cm. Find the ratio between the lengths of their corresponding sides.
- 2. A line PQ is drawn parallel to the base BC of Δ ABC which meets sides AB and AC at

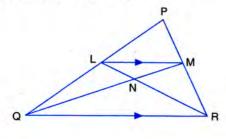
points P and Q respectively. If $AP = \frac{1}{3}PB$; find the value of :

- (i) $\frac{\text{Area of } \Delta \text{ ABC}}{\text{Area of } \Delta \text{ APQ}}$ Area of $\Delta \text{ APQ}$
- (ii) $\frac{\text{Area of } \Delta \text{ APQ}}{\text{Area of trapezium PBCQ}}$
- 3. The perimeters of two similar triangles are 30 cm and 24 cm. If one side of the first triangle is 12 cm, determine the corresponding side of the second triangle.
- 4. In the given figure, AX : XB = 3 : 5



Find :

- (i) the length of BC, if the length of XY is 18 cm.
- (ii) the ratio between the areas of trapezium XBCY and triangle ABC.
- 5. ABC is a triangle. PQ is a line segment intersecting AB in P and AC in Q such that PQ // BC and divides triangle ABC into two parts equal in area. Find the value of ratio BP : AB.
- 6. In the given triangle PQR, LM is parallel to QR and PM : MR = 3 : 4.



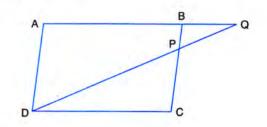
Calculate the value of ratio :

- (i) $\frac{PL}{PQ}$ and then $\frac{LM}{QR}$ (ii) $\frac{\text{Area of } \Delta \text{ LMN}}{\text{Area of } \Delta \text{ MNR}}$ (iii) $\frac{\text{Area of } \Delta \text{ LQM}}{\text{Area of } \Delta \text{ LQN}}$
- 7. The given diagram shows two isosceles triangles which are similar. In the given diagram, PQ and BC are not parallel; PC = 4, AQ = 3, QB = 12, BC = 15 and AP = PQ.

B

Calculate :

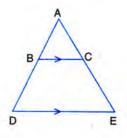
- (i) the length of AP,
 (ii) the ratio of the areas of triangle APQ and triangle ABC.
- 8. In the figure, given below, ABCD is a parallelogram. P is a point on BC such that BP : PC = 1 : 2. DP produced meets AB produced at Q. Given the area of triangle $CPQ = 20 \text{ cm}^2$.



Calculate :

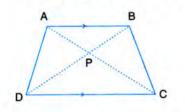
- (i) area of triangle CDP,
- (ii) area of parallelogram ABCD.
- 9. In the given figure, BC is parallel to DE. Area of triangle ABC = 25 cm², Area of trapezium BCED = 24 cm² and DE = 14 cm. Calculate the length of BC.

Also, find the area of triangle BCD.



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10. The given figure shows a trapezium in which AB is parallel to DC and diagonals AC and BD intersect at point P. If AP : CP = 3 : 5,

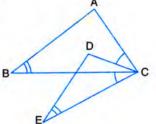


Find :

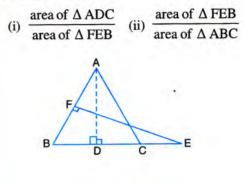
- (i) \triangle APB : \triangle CPB (ii) \triangle DPC : \triangle APB (iii) \triangle ADP : \triangle APB (iv) \triangle APB : \triangle ADB
- 11. In the given figure, ABC is a triangle. DE is parallel to BC and $\frac{AD}{DB} = \frac{3}{2}$.
 - (i) Determine the ratios $\frac{AD}{AB}$ and $\frac{DE}{BC}$.
 - (ii) Prove that Δ DEF is similar to Δ CBF.

Hence, find $\frac{EF}{FB}$.

- (iii) What is the ratio of the areas of \triangle DEF and \triangle BFC ? [2007]
- 12. In the given figure, $\angle B = \angle E$, $\angle ACD = \angle BCE$, AB = 10.4 cm and DE = 7.8 cm. Find the ratio between areas of the $\triangle ABC$ and $\triangle DEC$.



13. Triangle ABC is an isosceles triangle in which AB = AC = 13 cm and BC = 10 cm. AD is perpendicular to BC. If CE = 8 cm and $EF \perp AB$, find :

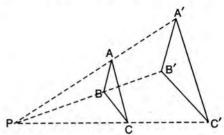


15.7 Similarity as a Size Transformation :

Draw a triangle ABC and mark a point P outside it.

Join P and A. Produce PA to point A' such that PA' = 2PA. Similarly, get PB' = 2PB and PC' = 2PC.

On joining A', B' and C'; we get another triangle A' B' C' which is similar to the original triangle ABC. If the sides of the triangle A' B' C' be measured and compared with the corresponding sides of the original triangle ABC, we find :



A' B' = 2AB, B'C' = 2BC and C'A' = 2CA.

Since, each side of the resulting triangle A' B' C' is twice the corresponding side of the original triangle ABC; $\Delta A'B'C'$ is similar to ABC and we say, that the triangle ABC has been enlarged by a scale factor 2 about the centre of enlargement P.

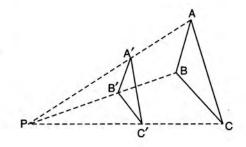
Similarly, if for the same triangle ABC and a point P outside it, we take a point A' in PA such that $PA' = \frac{1}{2}PA$; a point B' in PB such that $PB' = \frac{1}{2}PB$ and a point C' in

PC such that PC' = $\frac{1}{2}$ PC. On joining A', B' and C' we again get a triangle A' B' C' which is similar to the original triangle ABC.

On comparing the resulting triangle A' B' C' and the original triangle ABC, it will be observed that A' B' = $\frac{1}{2}$ AB B' C' = $\frac{1}{2}$ BC

observed that A' B' = $\frac{1}{2}$ AB, B' C' = $\frac{1}{2}$ BC

and C' A' = $\frac{1}{2}$ CA.



Since, each side of the resulting triangle A' B' C' is half of the corresponding side of the given triangle ABC; we say, that the triangle ABC has been reduced by a scale

factor
$$\frac{1}{2}$$
 about the centre of reduction P.

The type of enlargement or reduction, as discussed above, is called size transformation.

Thus in a size transformation, a given figure is enlarged or reduced by a scale factor k, such that the resulting figure (the image) is similar to the given figure (the object or the pre-image).

In a size transformation :

- (i) the image of a line is a line,
- (ii) the image of a triangle is a triangle,
- (iii) the image of a quadrilateral is a quadrilateral and so on.

15.8 Applications to Maps and Models :

Maps and Models : Students use different maps of India and of Asia in Geography. Consider the map of India in which the positions of its major cities are shown. Measure the distance between any two cities marked in the map and compare it with the actual distance between those two cities to get the ratio between the two distances. In the same way, choose two more cities marked in the map and compare their distance (on the map) with the actual distance between them to get the ratio between the two distances; we find that the ratio of distances in both the cases is the same.

In fact, this ratio is already marked (written) on every map and is known as scale factor which is denoted by letter, k'.

For Example :

If the scale of a map is 1 : 20,000, this implies that, a distance of one cm on the map is equal to an actual distance of 20,000 cm (0.2 km) on the ground. And, also scale factor $k = \frac{1}{20,000}$.

The same principle is applicable to models. In the case of models,

Height of the model		Length of the model
Height of the object	-	Length of the object
		Width of the model
	=	Width of the object
	=	Scale factor (k)

If the scale factor is k, then :

- (i) each side of the resulting figure (the image) is k times the corresponding side of the given figure (the object or the pre-image).
- (ii) the area of the resulting figure is k^2 times the area of the given figure.
- (iii) in the case of solids, the volume of the resulting figure is k^3 times the volume of the given figure.

(iv) $k > 1 \Rightarrow$ the transformation is an enlargement,

 $k < 1 \Rightarrow$ the transformation is a reduction and

 $k = 1 \Rightarrow$ the transformation is an identity transformation.

A model of a ship is made to a scale of 1 : 200. If the length of the model is 4 *m*; calculate the length of the ship.

Solution :

2

Clearly, the scale factor $k = \frac{1}{200}$ And, the length of model = k times the length of the ship. $4 m = \frac{1}{200} \times$ the length of the ship

⇒

 \Rightarrow

The length of the ship = 800 m

Ans.

The scale of map is 1 : 50,000. In the map, a triangular plot ABC of land has the following dimensions : AB = 2 cm, BC = 3.5 cm and angle ABC = 90°. Calculate : (i) the actual length of side BC, in km, of the land. (ii) the area of the plot in sq. km.

Solution :

 \Rightarrow

Clearly, scale factor $k = \frac{1}{50,000}$

(i) Length of side BC in the map = k times the actual length of side BC in the land.

$$3.5 \text{ cm} = \frac{1}{50,000} \times \text{actual length of BC}$$

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Actual length of BC = $50,000 \times 3.5$ cm

= 1.75 km

(ii) Since, the area of triangle ABC in the map = $\frac{1}{2} \times 2 \text{ cm} \times 3.5 \text{ cm}$

= 3.5 sq. cm

And, the area of \triangle ABC in the map = k^2 times the actual area of triangular plot ABC.

⇒

$$3.5 \text{ cm}^2 = \left(\frac{1}{50,000}\right)^2 \times \text{ actual area of the plot}$$

.

Actual area of the plot = $3.5 \times 50,000 \times 50,000$ sq. cm

= 0.875 sq. km

Ans.

Ans.

A rectangular tank has length = 4 m, width = 3 m and capacity = 30 m³. A small model of the tank is made with capacity 240 cm³. Find :

(i) the dimensions of the model.

(ii) the ratio between the total surface area of the tank and its model.

Solution :

For the tank :

Its length \times breadth \times height = Volume $4 \text{ m} \times 3 \text{ m} \times \text{height} = 30 \text{ m}^3$ \Rightarrow Height = $\frac{30}{4 \times 3}$ m = 2.5 m. \Rightarrow Let the scale factor for reduction = kVolume of the model = $k^3 \times$ volume of the tank ... $240 \text{ cm}^3 = k^3 \times 30 \text{ m}^3$ $240 \text{ cm}^3 = k^3 \times 30 \times 100 \times 100 \times 100 \text{ cm}^3$ \Rightarrow $k^3 = \frac{240}{30 \times 100 \times 100}$ \Rightarrow $=\frac{1}{125000}$ Scale factor, $k = \frac{1}{50}$ Length of the model = $k \times \text{length of the tank}$ (i) :. $=\frac{1}{50} \times 4 \text{ m} = 8 \text{ cm},$ breadth of the model = $k \times$ breadth of the tank $=\frac{1}{50} \times 3 \text{ m} = 6 \text{ cm}$

and, height of the model =
$$\frac{1}{50} \times 2.5 \text{ m} = 5 \text{ cm}$$

Dimensions of the model =
$$8 \text{ cm} \times 6 \text{ cm} \times 5 \text{ cm}$$

(ii) Since, total surface area of the model = $k^2 \times \text{total S.A.}$ of the tank

⇒

...

 $\frac{\text{Total S.A. of the tank}}{\text{Total S.A. of the model}} = \frac{1}{k^2} = (50)^2$

= 2500 = 2500 : 1

EXERCISE 15(D)

- 1. A triangle ABC has been enlarged by scale factor m = 2.5 to the triangle A' B' C' Calculate :
 - (i) the length of AB, if A' B' = 6 cm.
 - (ii) the length of C' A' if CA = 4 cm.
- 2. A triangle LMN has been reduced by scale factor 0.8 to the triangle L' M' N'. Calculate:
 - (i) the length of M' N', if MN = 8 cm.
 - (ii) the length of LM, if L' M' = 5.4 cm.
- 3. A triangle ABC is enlarged, about the point O as centre of enlargement, and the scale factor is 3. Find :
 - (i) A' B', if AB = 4 cm.
 - (ii) BC, if B' C' = 15 cm.
 - (iii) OA, if OA' = 6 cm.
 - (iv) OC', if OC = 21 cm.

Also, state the value of :

- (a) $\frac{OB'}{OB}$ (b) $\frac{C'A'}{CA}$
- 4. A model of an aeroplane is made to a scale of 1 : 400. Calculate :
 - (i) the length, in cm, of the model; if the length of the aeroplane is 40 m.
 - (ii) the length, in m, of the aeroplane, if length of its model is 16 cm.

- 5. The dimensions of the model of a multistorey building are 1.2 m × 75 cm × 2 m. If the scale factor is 1 : 30; find the actual dimensions of the building.
 6. On a map drawn to a scale of 1 : 2,50,000; a
- triangular plot of land has the following measurements : AB = 3 cm, BC = 4 cm and angle $ABC = 90^{\circ}$.

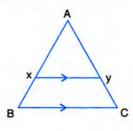
Calculate :

(i) the actual lengths of AB and BC in km.

- (ii) the area of the plot in sq. km.
- 7. A model of a ship is made to a scale of 1 : 200.
 - (i) The length of the model is 4 m; calculate the length of the ship.
 - (ii) The area of the deck of the ship is 160000 m²; find the area of the deck of the model.
 - (iii) The volume of the model is 200 litres; calculate the volume of the ship in m^3 .
- 8. An aeroplane is 30 m long and its model is 15 cm long. If the total outer surface area of the model is 150 cm², find the cost of painting the outer surface of the aeroplane at the rate of ₹ 120 per sq. m. Given that 50 sq. m of the surface of the aeroplane is left for windows.

EXERCISE 15(E)

1. In the following figure, XY is parallel to BC, AX = 9 cm, XB = 4.5 cm and BC = 18 cm.



Find :

(i)
$$\frac{AY}{YC}$$
 (ii) $\frac{YC}{AC}$ (iii) XY

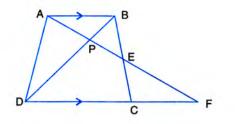
- 2. In the following figure, ABCD to a trapezium with AB // DC. If AB = 9 cm, DC = 18 cm, CF = 13.5 cm, AP = 6 cm and BE = 15 cm, Calculate :
 - (i) EC (ii) AF (iii) PE

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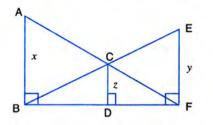
238

Ans.

Ans.



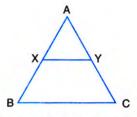
3. In the following figure, AB, CD and EF are perpendicular to the straight line BDF.



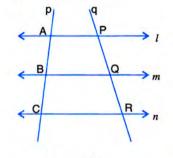
If AB = x and, CD = z unit and EF = y unit, prove that : $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$

Let BD = a and DF = b. In $\triangle ABF$, CD is parallel to AB $\Rightarrow \frac{CD}{AB} = \frac{DF}{BF}$ *i.e.*, $\frac{z}{x} = \frac{b}{a+b}$. And, in \triangle BEF, CD is parallel to EF $\Rightarrow \frac{CD}{EF} = \frac{BD}{BF}$ *i.e.* $\frac{z}{y} = \frac{a}{a+b}$. $\therefore \frac{z}{x} + \frac{z}{y} = \frac{b}{a+b} + \frac{a}{a+b} = 1$ $\Rightarrow \frac{1}{x} + \frac{1}{y} = \frac{1}{z}$

- 4. Triangle ABC is similar to triangle PQR. If AD and PM are corresponding medians of the two triangles, prove that : $\frac{AB}{PQ} = \frac{AD}{PM}$.
- 5. Triangle ABC is similar to triangle PQR. If AD and PM are altitudes of the two triangles, prove that : $\frac{AB}{PQ} = \frac{AD}{PM}$.
- 6. Triangle ABC is similar to triangle PQR. If bisector of angle BAC meets BC at point D and bisector of angle QPR meets QR at point M, prove that : $\frac{AB}{PQ} = \frac{AD}{PM}$.
- 7. In the following figure, $\angle AXY = \angle AYX$.
 - If $\frac{BX}{AX} = \frac{CY}{AY}$, show that triangle ABC is isosceles.

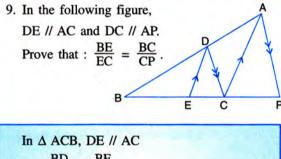


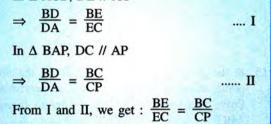
8. In the following diagram, lines *l*, *m* and *n* are parallel to each other. Two transversals *p* and *q* intersect the parallel lines at points A, B, C and P, Q, R as shown.



Prove that :
$$\frac{AB}{BC} = \frac{PQ}{QR}$$

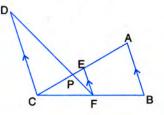
Join A and R. Let AR meets BQ at point D.





10. In the figure given below, AB // EF // CD. If AB = 22.5 cm, EP = 7.5 cm, PC = 15 cm and DC = 27 cm.

Calculate : (i) EF (ii) AC



11. In quadrilateral ABCD, its diagonals AC and BD intersect at point O such that

$$\frac{OC}{OA} = \frac{OD}{OB} = \frac{1}{3}$$
.

Prove that :

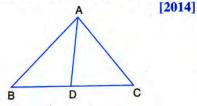
- (i) $\Delta OAB \sim \Delta OCD$
- (ii) ABCD is a trapezium.Further if CD = 4.5 cm; find the length of AB.
- 12. In triangle ABC, angle A is obtuse and AB = AC. P is any point in side BC. PM \perp AB and PN \perp AC.

Prove that : $P M \times PC = PN \times PB$

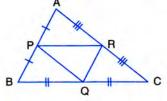
13. In triangle ABC, AB = AC = 8 cm, BC = 4 cm and P is a point in side AC such that AP = 6 cm. Prove that Δ BPC is similar to Δ ABC. Also, find the length of BP.

In $\triangle ABC$, $\frac{AB}{BC} = \frac{8}{4} = 2$, in $\triangle BPC$, $\frac{BC}{CP} = \frac{4}{2} = 2$ and $\angle ABC = \angle C$. Therefore, by SAS, $\triangle ABC$ is similar to $\triangle BPC$.

- 14. In $\triangle ABC$, $\angle ABC = \angle DAC$, AB = 8 cm, AC = 4 cm and AD = 5 cm.
 - (i) Prove that $\triangle ACD$ is similar to $\triangle BCA$.
 - (ii) Find BC and CD.
 - (iii) Find area of $\triangle ACD$: area of $\triangle ABC$.



15. In the given triangle P, Q and R are the midpoints of sides AB, BC and AC respectively. Prove that triangle PQR is similar to triangle ABC.



F

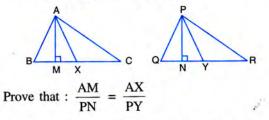
D

 In the following figure, AD and CE are medians of Δ ABC. DF is drawn parallel to CE. Prove that :

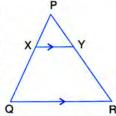
(i) EF = FB,

(ii) AG : GD = 2 : 1.

17. In the given figure, triangle ABC is similar to triangle PQR. AM and PN are altitudes whereas AX and PY are medians.



- 18. The two similar triangles are equal in area. Prove that the triangles are congruent.
- 19. The ratio between the altitudes of two similar triangles is 3 : 5; write the ratio between their :(i) medians. (ii) perimeters. (iii) areas.
- 20. The ratio between the areas of two similar triangles is 16 : 25. Find the ratio between their :
 - (i) perimeters. (ii) altitudes. (iii) medians.
- 21. The given figure shows a triangle PQR in which XY is parallel to QR. If PX : XQ = 1 : 3 and QR = 9 cm, find the length of XY.



Further, if the area of $\Delta PXY = x \text{ cm}^2$; find, in terms of x, the area of :

- (i) triangle PQR. (ii) trapezium XQRY.
- 22. On a map, drawn to a scale of 1 : 20000, a rectangular plot of land ABCD has AB = 24 cm and BC = 32 cm. Calculate :
 - (i) the diagonal distance of the plot in kilometre.
 - (ii) the area of the plot in sq. km.
- 23. The dimensions of the model of a multistoreyed building are 1 m by 60 cm by 1.20 m. If the scale factor is 1:50, find the actual dimensions of the building.

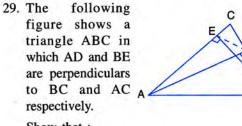
Also, find :

- (i) the floor area of a room of the building, if the floor area of the corresponding room in the model is 50 sq. cm.
- (ii) the space (volume) inside a room of the model, if the space inside the corresponding room of the building is 90 m³.

- 24. In a triangle PQR, L and M are two points on the base QR, such that $\angle LPQ = \angle QRP$ and $\angle RPM = \angle RQP$. Prove that :
 - (i) \triangle PQL ~ \triangle RPM (ii) QL × RM = PL × PM (iii) PQ² = QR × QL Q L M R [2003]
- 25. In \triangle ABC, \angle ACB = 90° and CD \perp AB. Prove that : $\frac{BC^2}{AC^2} = \frac{BD}{AD}$.
- 26. A triangle ABC with AB = 3 cm, BC = 6 cm and AC = 4 cm is enlarged to Δ DEF such that the longest side of Δ DEF = 9 cm. Find the scale factor and hence, the lengths of the other sides of Δ DEF.
- 27. Two isosceles triangles have equal vertical angles. Show that the triangles are similar.

If the ratio between the areas of these two triangles is 16 : 25, find the ratio between their corresponding altitudes.

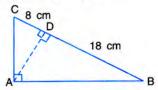
- 28. In \triangle ABC, A AP : PB = 2 : 3. PO is parallel to BC and is extended to Q so that CQ is parallel to BA. Find :
 - (i) area Δ APO : area Δ ABC.
 - (ii) area \triangle APO : area \triangle CQO.



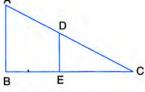
Show that :

- (i) \triangle ADC ~ \triangle BEC
- (ii) $CA \times CE = CB \times CD$
- (iii) \triangle ABC ~ \triangle DEC
- (iv) $CD \times AB = CA \times DE$
- 30. In the given figure, ABC is a triangle with ∠EDB = ∠ACB. Prove that Δ ABC ~ Δ EBD.
 If BE = 6 cm, EC = 4 cm, BD = 5 cm and area of Δ BED = 9 cm². Calculate the :
 (i) length of AB

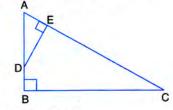
- (ii) area of \triangle ABC \overrightarrow{A} B E C [2010]
- 31. In the given figure, ABC is a right angled triangle with $\angle BAC = 90^{\circ}$.



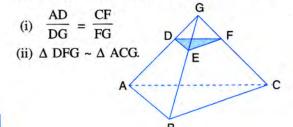
- (i) Prove that : $\triangle ADB \sim \triangle CDA$.
- (ii) If BD = 18 cm and CD = 8 cm, find AD.
- (iii) Find the ratio of the area of $\triangle ADB$ is to area of $\triangle CDA$. [2011]
- 32. In the given figure, AB and DE are perpendiculars to BC.



- (i) Prove that : $\triangle ABC \sim \triangle DEC$
- (ii) If AB = 6 cm, DE = 4 cm and AC = 15 cm. Calculate CD.
- (iii) Find the ratio of the area of a \triangle ABC : area of \triangle DEC. [2013]
- 33. ABC is a right angled triangle with \angle ABC = 90°. D is any point on AB and DE is perpendicular to AC. Prove that :



- (i) $\triangle ADE \sim \triangle ACB$.
- (ii) If AC = 13 cm, BC = 5 cm and AE = 4 cm. Find DE and AD.
- (iii) Find, area of $\triangle ADE$: area of quadrilateral BCED. [2015]
- 34. Given : AB // DE and BC // EF. Prove that :



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